

# A Pyrrhic Victory? – Bank Bailouts and Sovereign Credit Risk<sup>1</sup>

Viral V. Acharya<sup>2</sup>  
NYU-Stern, CEPR and NBER

Itamar Drechsler<sup>3</sup>  
NYU-Stern

Philipp Schnabl<sup>4</sup>  
NYU-Stern and CEPR

J.E.L. Classification: G21, G28, G38, E58, D62.

Keywords: financial crises, forbearance, sovereign debt, credit default swaps, growth

First draft: August 2010

This draft: July 2011

<sup>1</sup>We are grateful to Ilan Kremer, Mitchell Petersen, Isabel Schnabel and Luigi Zingales (discussants), Dave Backus, Mike Chernov, Amir Yaron, Stan Zin, and seminar participants at the 2011 American Economic Association Meetings, Austrian Central Bank, Bundesbank-ECB-CFS Joint Luncheon workshop, Douglas Gale's Financial Economics workshop at NYU, Federal Reserve Bank of Minneapolis, HEC Paris and BNP Paribas Hedge Fund Center conference, Indian School of Business, Indian Institute of Management (Ahmedabad), London Business School and Moody's Credit Risk Conference, Oxford Said Business School, Rothschild Caesarea Center 8th Annual Conference (Israel), Stockholm School of Economics and SIFR, Universitat van Amsterdam and de Nederlandsche Bank, and University of Minnesota for helpful comments. Farhang Farazmand and Nirupama Kulkarni provided valuable research assistance.

<sup>2</sup>Department of Finance, Stern School of Business, New York University, e-mail: vacharya@stern.nyu.edu

<sup>3</sup>Department of Finance, Stern School of Business, New York University, e-mail: itamar.drechsler@stern.nyu.edu.

<sup>4</sup>Department of Finance, Stern School of Business, New York University, e-mail: schnabl@stern.nyu.edu.

# A Pyrrhic Victory? – Bank Bailouts and Sovereign Credit Risk

## Abstract

We show that financial sector bailouts and sovereign credit risk are intimately linked. A bailout benefits the economy by ameliorating the under-investment problem of the financial sector. However, increasing taxation of the non-financial sector to fund the bailout may be inefficient since it weakens its incentive to invest, decreasing growth. Instead, the sovereign may choose to fund the bailout by diluting existing government bondholders, resulting in a deterioration of the sovereign's creditworthiness. This deterioration feeds back onto the financial sector, reducing the value of its guarantees and existing bond holdings and increasing its sensitivity to future sovereign shocks. We provide empirical evidence for this two-way feedback between financial and sovereign credit risk using data on the credit default swaps (CDS) of the Eurozone countries for 2007-10. We show that the announcement of financial sector bailouts was associated with an immediate, unprecedented widening of sovereign CDS spreads and narrowing of bank CDS spreads; however, post-bailouts there emerged a significant co-movement between bank CDS and sovereign CDS, even after controlling for banks' equity performance, the latter being consistent with an effect of the quality of sovereign guarantees on bank credit risk.

J.E.L. Classification: G21, G28, G38, E58, D62.

Keywords: financial crises, forbearance, sovereign debt, credit default swaps, growth

# 1 Introduction

Just two and a half years ago, there was essentially no sign of sovereign credit risk in the developed economies and a prevailing view was that this was unlikely to be a concern for them in the near future. Recently, however, sovereign credit risk has become a significant problem for a number of developed countries. In this paper, we are motivated by three closely related questions surrounding this development. First, were the financial sector bailouts an integral factor in igniting the rise of sovereign credit risk in the developed economies? We show that they were. Second, what was the exact mechanism that caused the transmission of risks between the financial sector and the sovereign? We propose a theoretical explanation wherein the government can finance a bailout through both increased taxation and via dilution of existing government debt-holders. The bailout is beneficial; it alleviates a distortion in the provision of financial services. However, both financing channels are costly. Increased taxation reduces the non-financial sector's incentives to invest. When the optimal bailout is large this implies that dilution can become a relatively attractive option, even though it leads to deterioration in the sovereign's creditworthiness. Finally, we ask whether there is also feedback going in the other direction— does sovereign credit risk feedback on to the financial sector? We explain – and verify empirically – that such a feedback is indeed present, due to the financial sector's implicit and explicit guarantees and holdings of sovereign bonds.

Our results call into question the usually implicit assumption that government resources are vastly deep and that the main problem posed by bailouts is that of moral hazard – that is, the distortion of future financial sector incentives. While the moral hazard cost is certainly pertinent, our conclusion is that bailout costs are not just in the future. They are tangible right around the timing of bailouts and are priced into the sovereign's credit risk and cost of borrowing. Thus, aggressive bailout packages that stabilize financial sectors in the short run but ignore the ultimate taxpayer cost might end up being a Pyrrhic victory.

**Motivation: The case of Irish bailout.** On September 30, 2008 the government of Ireland announced that it had guaranteed all deposits of the six of its biggest banks. The immediate reaction that grabbed newspaper headlines the next day was whether such a policy of a full savings guarantee was anti-competitive in the Euro area. However, there was something deeper manifesting itself in the credit default swap (CDS) markets for purchasing protection against the sovereign credit risk of Ireland and that of its banks. Figure 1 shows that while the cost of purchasing such protection on Irish banks – their CDS fee – fell overnight from around 400 basis points (bps) to 150 bps, the CDS fee for the Government of Ireland's credit

risk rose sharply. Over the next month, this rate more than quadrupled to over 100 bps and within six months reached 400 bps, the starting level of its financial firms' CDS. While there was a general deterioration of global economic health over this period, the event-study response in Figure 1 suggests that the risk of the financial sector had been substantially transferred to the government balance sheet, a cost that Irish taxpayers must eventually bear.

Viewed in the Fall of 2010, this cost rose to dizzying heights prompting economists to wonder if the precise manner in which bank bailouts were awarded have rendered the financial sector rescue exorbitantly expensive. Just one of the Irish banks, Anglo Irish, has cost the government up to Euro 25 bln (USD 32 bln), amounting to 11.26% of Ireland's Gross Domestic Product (GDP). Ireland's finance minister Brian Lenihan justified the propping up of the bank "to ensure that the resolution of debts does not damage Ireland's international credit-worthiness and end up costing us even more than we must now pay." Nevertheless, rating agencies and credit markets revised Ireland's ability to pay future debts significantly downward. The original bailout cost estimate of Euro 90 bln was re-estimated to be 50% higher and the Irish 10-year bond spread over German bund widened significantly, ultimately leading to a bailout of Irish government by the stronger Eurozone countries.<sup>1</sup>

This episode is not isolated to Ireland though it is perhaps the most striking case. In fact, a number of Western economies that bailed out their banking sectors in the Fall of 2008 have experienced, in varying magnitudes, similar risk transfer between their financial sector and government balance-sheets. Our paper develops a theoretical model and provides empirical evidence that help understand this interesting phenomenon.

**Model.** Our theoretical model consists of two sectors of the economy – "financial" and "corporate" (more broadly this includes also the household and other non-financial parts of the economy), and a government. The two sectors contribute jointly to produce aggregate output: the corporate sector makes productive investments and the financial sector invests in intermediation "effort" (e.g., information gathering and capital allocation) that enhance the return on corporate investments. Both sectors, however, face a potential under-investment problem. The financial sector is leveraged (in a crisis, it may in fact be insolvent) and under-invests in its contributions due to the well-known debt overhang problem (Myers, 1977). We assume that restructuring this financial sector debt is impossible or prohibitively

---

<sup>1</sup>See "Ireland's banking mess: Money pit – Austerity is not enough to avoid scrutiny by the markets", the Economist, Aug 19th 2010; "S&P downgrades Ireland" by Colin Barr, CNNMoney.com, Aug 24th 2010; and, "Ireland stung by S&P downgrade", Reuters, Aug 25th, 2010.

expensive. For simplicity, the corporate sector is un-levered. However, if the government undertakes a “bailout” of the financial sector, in other words, makes a transfer from the rest of the economy that results in a net reduction of the financial sector debt, then the transfer must be funded in the future (at least in part) through taxation of corporate profits. Such taxation, assumed to be proportional to corporate sector output, induces the corporate sector to under-invest.

A government that is fully aligned with maximizing the economy’s current and future output determines the optimal size of the bailout. We show that tax proceeds that can be used to fund the bailout have, in general, a *Laffer curve* property, so that the optimal bailout size and tax rate are interior. The optimal tax rate that the government is willing to undertake for the bailout is greater when the financial sector’s debt overhang is higher and its relative contribution (or size) in output of the economy is larger.

In practice, governments fund bailouts in the short run by borrowing or issuing bonds, which are repaid by future taxation. There are two interesting constraints on the bailout size that emerge from this observation. One, the greater is the legacy debt of the government, the lower is its ability to undertake a bailout. This is because the Laffer curve of tax proceeds leaves less room for the government to increase tax rates for repaying its bailout-related debt. Second, the announcement of the bailout lowers the price of government debt due to the anticipated dilution from newly issued debt. Now, if the financial sector of the economy has assets in place that are in the form of government bonds, the bailout is in fact associated with some “collateral damage” for the financial sector itself. Illustrating the possibility of such a two-way feedback is a novel contribution of our model.

To get around these constraints, the government can potentially undertake a *strategic* default. Assuming that there are some deadweight costs of such default, for example, due to international sanctions or from being unable to borrow in debt markets for some time, we derive the optimal boundary for sovereign default as a function of its legacy debt and financial sector liabilities. This boundary explains that a heavily-indebted sovereign faced with a heavily-insolvent financial sector will be forced to “sacrifice its credit rating” to save the financial sector and at the same time sustain economic growth.

We then extend the model to allow for uncertainty about the realized output growth of the corporate sector. This introduces a possibility of *solvency*-based default on government debt. Interestingly, given the collateral damage channel, an increase in uncertainty about the sovereign’s economic output not only lowers its own debt values but also increases the financial sector’s risk of default. This is because the financial sector’s government bond

holdings fall in value, and in an extension of the model, so do the value of the government guarantees accorded to the financial sector as a form of bailout. In turn, these channels induce a post-bailout co-movement between the financial sector's credit risk and that of the sovereign, even though the immediate effect of the bailout is to lower the financial sector's credit risk and raise that of the sovereign.

**Empirics.** Our empirical work analyzes this two-way feedback between the financial sector and sovereign credit risk. Our analysis focuses mainly on the Western European economies during the financial crisis of 2007-10.

We examine sovereign and bank CDS in the period from 2007 to 2010 and find three distinct periods. The first period covers the start of the financial crisis in January 2007 until the first bank bailout announcement. This period includes the bankruptcy of Lehman Brothers. Across all Western economies, we see a large, sustained rise in bank CDS as the financial crisis develops. However, sovereign CDS spreads remain very low. This evidence is consistent with a significant increase in the default risk of the banking sector with little effect on sovereigns in the pre-bailout period.

The second period covers the bank bailouts starting with the announcement of a bailout in Ireland in late September 2008 and ending with a bailout in Sweden in late October 2008. During this one-month period, we find a significant decline in bank CDS across all countries and a corresponding increase in sovereign CDS. This evidence suggests that bank bailouts produced a transfer of default risk from the banking sector to the sovereign.

The third period covers the period after the bank bailouts and until 2010. We find that both sovereign and bank CDS increased during this period. The increase was larger for countries whose public debt ratios were higher and whose financial sectors were more distressed in the pre-bailout period. Consistent with our models' prediction of bailout-induced dilution of debtholders, we also find that there emerges post-bailouts a strong, positive relationship between public debt ratios and sovereign CDS, though none existed beforehand. This evidence supports our view that the bailouts spilled banks' credit risk onto the sovereigns and triggered the rise in sovereign credit risk.

We then carry out a series of empirical tests to document and quantify the *direct* two-way feedback between sovereign and financial credit risk emphasized by our model. The tests show that in the post-bailout period an increase in sovereign credit risk is associated with a robust and economically significant increase in the credit risk of that country's banks, even after controlling for market-wide shocks to credit risk, volatility, 'local' CDS-market conditions, common variation in bank CDS, and changes in bank-level fundamentals. The

additional impact of sovereign risk beyond these extensive controls arises because of the special subsidy that government guarantees provide to debt-holders, allowing us to empirically establish the sovereign-bank feedback.

Finally, in support of the collateral damage channel as being potentially relevant for the co-movement between financial sector and sovereign CDS, we collect bank-level data on holdings of different sovereign government bonds released as part of the stress tests conducted for European banks in 2010. We document that on average Eurozone banks stress-tested in 2010 had Eurozone government bond holdings that were as large as one-sixth of their risk-weighted assets. We also find that bank CDS co-moves with sovereign CDS in accordance with banks' holdings of government bonds.

The remainder of the paper is organized as follows. Section 2 sets up the model. Section 3 presents the equilibrium outcomes. Section 4 provides empirical evidence and in conclusion also discusses the case of Iceland as a possible counterfactual for the case of Ireland. Section 5 relates our theoretical and empirical analysis to the extant literature. Section 6 concludes. All proofs not in the main text are in the online Appendix.

## 2 Model

There are three time periods in the model:  $t = 0, 1$ , and 2. The productive economy consists of two parts, a financial sector and a non-financial sector. In addition, there is a government and a representative consumer. All agents are risk-neutral.

**Financial sector:** The operator of the financial sector solves the following problem, which is to choose, at  $t = 0$ , the amount of financial services to supply at  $t = 1$  in order to maximize his expected payoff at  $t = 1$ , net of the effort cost required to produce these services:

$$\max_{s_0^s} E_0 \left[ \left( w_s s_0^s - L_1 + \tilde{A}_1 + A_G + T_0 \right) \times 1_{\{-L_1 + \tilde{A}_1 + A_G + T_0 > 0\}} \right] - c(s_0^s) \quad . \quad (1)$$

where  $s_0^s$  is the amount of financial services supplied by the financial sector at  $t = 1$ . The financial sector earns revenues at the rate of  $w_s$  per unit of financial service supplied, with  $w_s$  determined in equilibrium. To produce  $s_0$  units, the operator of the financial sector expends  $c(s_0)$  units of effort. We assume that  $c'(s_0) > 0$  and  $c''(s_0) > 0$ .

The financial sector has both liabilities and assets on its books. It receives the payoff from its efforts only if the value of assets exceeds liabilities at  $t = 1$ . This solvency condition is given in equation (1) by the indicator function for the expression  $-L_1 + \tilde{A}_1 + A_G + T_0 > 0$ .

$L_1$  denotes the liabilities of the financial sector, which are due (mature) at  $t = 1$ . There are two types of assets held by the financial sector, denoted  $\tilde{A}_1$  and  $A_G$ .  $A_G$  is the value of the financial sector's holdings of a fraction  $k_A$  of the existing (pre-bailout) stock of government bonds, while  $\tilde{A}_1$  represents the payoff of the other assets held by the financial sector.<sup>2</sup> We model the payoff  $\tilde{A}_1$ , which is risky, as a continuously valued random variable that is realized at  $t = 1$  and takes values in  $[0, \infty)$ . The payoff and value of government bonds is discussed below. The variable  $T_0$  represents the value of the time 0 transfer made by the government to the financial sector and is discussed further below. Finally, in case of insolvency, debtholders receive ownership of all financial sector assets and wage revenue.<sup>3</sup>

**Non-financial sector:** The non-financial sector comes into  $t = 0$  with an existing capital stock  $K_0$ . Its objective is to maximize the sum of the expected values of its net payoffs, which occur at  $t = 1$  and  $t = 2$ :

$$\max_{s_0^d, K_1} E_0 \left[ f(K_0, s_0^d) - w_s s_0^d + (1 - \theta_0) \tilde{V}(K_1) - (K_1 - K_0) \right] \quad (2)$$

The function  $f$  is the production function of the non-financial sector, which takes as inputs at  $t = 0$  the financial services it demands,  $s_0^d$ , and the capital stock,  $K_0$ , to produce consumption goods at  $t = 1$ . The output of  $f$  is deterministic and  $f$  is increasing in both arguments and concave. At  $t = 1$ , the non-financial sector is faced with a decision of how much capital  $K_1$  to invest, at an incremental cost of  $(K_1 - K_0)$ , in a project  $\tilde{V}$ , whose payoff is realized at  $t = 2$ . This project represents the future or continuation value of the non-financial sector and is in general subject to uncertainty. The expectation at  $t = 1$  of this payoff is  $V(K_1) = E_1[\tilde{V}(K_1)]$  and, as indicated, is a function of the investment  $K_1$ . We assume that  $V'(K_1) > 0$  and  $V''(K_1) < 0$ , so that the expected payoff is increasing but concave in investment. A proportion  $\theta_0$  of the payoff of the continuation project is taxed by the government to pay its debt, both new and outstanding, as we explain next.

**Government:** The government's objective is to maximize the total output of the economy and hence the welfare of the consumer. It does this by reducing the debt-overhang problem of the financial sector, which induces it to supply more financial services, thereby increasing

---

<sup>2</sup>While we refer to government claims principally as government bonds, a broader interpretation can include claims on quasi-governmental agencies (e.g., Fannie Mae, Freddie Mac) and also the value of different types of government subsidies or support.

<sup>3</sup>We could include wage revenues in the solvency indicator function, which would provide an additional channel for wages to feed back into the probability of solvency. Although such a channel would reinforce the mechanism at work in the model, we choose to abstract from this to avoid the additional complexity.



output. To achieve this, the government issues bonds that it then transfers to the balance sheet of the financial sector. These bonds are repaid with taxes levied on the non-financial sector at a tax-rate of  $\theta_0$ .<sup>4</sup> In particular, the tax rate  $\theta_0$  is set by the government at  $t = 0$  and is levied at  $t = 2$  upon realization of the payoff  $\tilde{V}(K_1)$ . We assume that the government credibly commits to this tax rate.

We let  $N_D$  denote the number of bonds that the government has issued in the past – its outstanding stock of debt. For simplicity, bonds have a face value of one, so the face value of outstanding debt equals the number of bonds,  $N_D$ . The government issues  $N_T$  new bonds to accomplish the transfer to the financial sector. Hence, at  $t = 2$  the government receives realized taxes equal to  $\theta_0 \tilde{V}(K_1)$  and then uses them to pay bondholders  $N_T + N_D$ . We assume that if there are still tax revenues left over (a surplus), the government spends them on programs for the representative consumer, or equivalently, just rebates them to the consumer. On the other hand, if tax revenues fall short of  $N_T + N_D$ , then the government defaults on its debt. In that case, it pays out all the tax revenue raised to bondholders. We assume that the government credibly commits to this payout policy.<sup>5</sup>

We further assume that default incurs a deadweight loss. In case of default, the sovereign incurs a fixed deadweight loss of  $D$ . Hence, default is costly and there is an incentive to avoid it.<sup>6</sup> Finally, let  $P_0$  denote the price of government bonds, which is determined in equilibrium.

The government's objective is to maximize the expected utility of the representative consumer, who consumes the combined output of the financial and non-financial sector. Hence, the government faces the following problem:

$$\max_{\theta_0, N_T} E_0 \left[ f(K_0, s_0) + \tilde{V}(K_1) - c(s_0) - (K_1 - K_0) - 1_{def}D + \tilde{A}_1 \right] \quad (3)$$

where  $s_0$  is the equilibrium provision of financial services. This maximization is subject to the budget constraint:  $T_0 = P_0 N_T$  and subject to the choices made by the financial and non-financial sectors. Note that  $1_{def}$  is an indicator function that equals 1 if the government defaults (if  $\theta_0 \tilde{V}(K_1) < N_T + N_D$ ) and 0 otherwise.

---

<sup>4</sup>Issuing bonds that are repaid with future taxes allows the government to smooth taxation over time. We do not model the tax-smoothing considerations here but note that tax-smoothing would be optimal if, for example, there is a convex cost of taxation in each time period.

<sup>5</sup>We can consider more generally a policy whereby the government pays only a fraction  $\tilde{m}$  of tax revenue and gives back any remaining tax funds to the consumer. Since it will actually be optimal for the government to commit to paying bondholders all the tax revenue raised, we restrict ourselves to the case  $\tilde{m} = 1$ .

<sup>6</sup>Although  $D$  here is obviously reduced-form, one can think of the deadweight cost in terms of loss of government reputation internationally, loss of domestic government credibility, degradation of the legal system and so forth. If a country's reputation is already weak, it will have less to lose from default.

**Consumer:** The representative consumer consumes the output of the economy. He solves a simple consumption and portfolio choice problem by allocating his wealth  $W$  between consumption, government bond holdings, and equity in the financial and non-financial sectors. Since the representative consumer is assumed to be risk-neutral and there is no time discounting, asset prices equal the expected values of asset payouts. Let  $P(i)$  and  $\tilde{P}(i)$  denote the price and payoff of asset  $i$ , respectively. At  $t = 0$ , the consumer chooses optimal portfolio allocations,  $\{n_i\}$ , that solve the following problem:

$$\max_{n_i} E_0 \left[ \Sigma_i n_i \tilde{P}(i) + (W - \Sigma_i n_i P(i)) \right] \quad (4)$$

The consumer's first order condition gives the standard result that equilibrium price of an asset equals the expected value of its payoff,  $P(i) = E_0[\tilde{P}(i)]$ .

### 3 Equilibrium Outcomes

We begin by examining the maximization problem of the financial sector. Let  $p(\tilde{A})$  denote the probability density of  $\tilde{A}$ . Furthermore, let  $\underline{A}_1$  be the minimum realization of  $\tilde{A}_1$  for which the financial sector does not default:  $\underline{A}_1 = L_1 - A_G - T_0$ . Then, the first order condition of the financial sector can be written as:

$$w_s p_{solv} - c'(s_0^s) = 0 . \quad (5)$$

where  $p_{solv} \equiv \int_{\underline{A}_1}^{\infty} p(\tilde{A}_1) d\tilde{A}$ , is the probability that the financial sector is solvent at  $t = 1$ . Henceforth, we parameterize  $c(s_0)$  as follows:  $c(s_0) = \beta \frac{1}{m} s_0^m$  where  $m > 1$ .

Consider now the problem of the non-financial sector at  $t = 0$ . Its demand for financial services,  $\hat{s}_0^d$ , is determined by its first-order condition:<sup>7</sup>

$$\frac{\partial f(K_0, s_0^d)}{\partial s_0^d} = w_s . \quad (6)$$

We parameterize  $f$  as Cobb-Douglas with the factor share of financial services given by  $\vartheta$ :  $f(K_0, s_0) = \alpha K_0^{1-\vartheta} s_0^\vartheta$ .

In equilibrium the demand and supply of financial services are the same:  $\hat{s}_0^d = \hat{s}_0^s$ . From

---

<sup>7</sup>Both the second-order conditions of the financial and non-financial sectors are satisfied:  $-c''(s_0) < 0$  and  $\frac{\partial^2 f(K_0, s_0^d)}{\partial^2 s_0^d} < 0$ .

here on, we drop the superscripts and denote the equilibrium quantity of financial services simply by  $s_0$ .

### 3.1 Transfer Reduces Underprovision of Financial Services

Taken together, the first-order conditions of the financial sector (5) and non-financial sector (6) show how debt-overhang impacts the provision of financial services by the financial sector. The marginal benefit of an extra unit of financial services to the economy is given by  $w_s$ , while the marginal cost,  $c'(s_0)$ , is less than  $w_s$  if there is a positive probability of insolvency. This implies that the equilibrium allocation is sub-optimal. The reason is that the possibility of liquidation  $p_{solv} < 1$  drives a wedge between the social and private marginal benefit of an increase in the provision of financial services. As long as  $p_{solv} < 1$ , there is an under-provision of financial services relative to the first-best case ( $p_{solv} = 1$ ). Hence, we obtain that

**Lemma 1.** *An increase in the transfer  $T_0$  leads to an increase in the provision of financial services since this raises the probability  $p_{solv}$  that the financial sector is solvent at  $t = 1$ .*

### 3.2 Tax Revenues: A Laffer Curve

Next, to understand the government's problem, we first look at how expected tax revenue responds to the tax rate,  $\theta_0$ . Let the expected tax revenue,  $\theta_0 V(K_1)$ , be denoted by  $\mathcal{T}$ . Raising taxes has two effects. On the one hand, an increase in the tax rate  $\theta_0$  captures a larger proportion of the future value of the non-financial sector, thereby raising tax revenues. On the other hand, this reduces the incentive of the non-financial sector to invest in its future, thereby leading to reduced investment,  $K_1$ . At the extreme, when  $\theta_0 = 1$ , the tax distortion eliminates the incentive for investment and tax revenues are reduced to zero. Hence, tax revenues are non-monotonic in the tax rate and maximized by a tax rate strictly less than 1.

Formally, the impact on tax revenue of an increase in the tax rate is given by:

$$\frac{d\mathcal{T}}{d\theta_0} = V(K_1) + \theta_0 V'(K_1) \frac{dK_1}{d\theta_0} \quad .$$

Note that at  $\theta_0 = 0$ , an increase in the tax rate increases the tax revenue at a rate equal to  $V(K_1)$ , the future value of the non-financial sector. It can be shown that since the production function  $V(K_1)$  is concave, as taxes are increased the incentive to invest is decreased by the tax rate, which reduces the marginal revenue of a tax increase. To see this, consider the

first-order condition for investment of the non-financial sector at  $t = 1$ :

$$(1 - \theta_0)V'(K_1) - 1 = 0 \quad . \quad (7)$$

Taking the derivative with respect to  $\theta_0$  using the Implicit Function theorem gives:  $\frac{dK_1}{d\theta_0} = \frac{V'(K_1)}{(1-\theta_0)V''(K_1)} < 0$ , which shows that as the tax rate is increased, the non-financial sector reduces investment.<sup>8</sup> Since at  $\theta_0 = 1$  the tax revenue is zero this implies that the marginal tax revenue decreases until it eventually becomes negative. Hence, tax revenues satisfy the Laffer curve property as a function of the tax rate:

**Lemma 2.** *The tax revenues,  $\theta_0 V(K_1)$ , increase in the tax rate,  $\theta_0$ , as it increases from zero (no taxes), and then eventually decline.*

Henceforth, we parameterize  $V$  with the functional form  $V(K_1) = K_1^\gamma$ ,  $0 < \gamma < 1$ .<sup>9</sup> As Appendix A.3 shows, (7) implies that  $\mathcal{T} = \theta_{t+1}\gamma^{1-\gamma}(1-\theta_{t+1})^{\frac{\gamma}{1-\gamma}}$ . It can then be shown that:

**Lemma 3.** *The tax revenue,  $\mathcal{T}$ , is maximized at  $\theta_0^{max} = 1 - \gamma$ , is increasing ( $d\mathcal{T}/d\theta_0 > 0$ ) and concave ( $d^2\mathcal{T}/d\theta_0^2 < 0$ ) on  $[0, \theta_0^{max})$ , and decreasing ( $d\mathcal{T}/d\theta_0 < 0$ ) on  $(\theta_0^{max}, 1)$ .*

### 3.3 Optimal Transfer Under Certainty and No Default

We analyze next the government's decision starting first with a simplified version of the general setup. We make two simplifying assumptions: (1) we set to zero the variance of the realized future value of the non-financial sector, so that  $\tilde{V}(K_1) = V(K_1)$ , (2) we force the government to remain solvent. In subsequent sections we remove these assumptions.

If the government must remain solvent, it can only issue a number of bonds  $N_T$  that it can pay off in full, given its tax revenue. By assumption (1), the tax revenue is known exactly (it is equal to  $\mathcal{T}$ ), and hence by assumption (2),  $N_T + N_D = \mathcal{T}$ . Moreover, since every bond has a sure payoff of 1, we know that the bond price is  $P_0 = 1$ .

---

<sup>8</sup>While we have chosen to model the tax-induced distortion in investment, a tax on the non-financial sector's labor income would have a similar effect if the sector makes a labor-leisure trade-off. In that case, the tax on labor income decreases the marginal benefit from labor, thereby reducing the equilibrium labor choice and resulting output. More generally, we may broadly interpret the investment  $K_1$  as going beyond investment in capital to include e.g., the investment of entrepreneurial effort and other human capital.

<sup>9</sup>This functional form is a natural choice for an increasing and concave function of  $K_1$ . Appendix A.2 provides a more structural motivation for this choice based on the calculation of a continuation value under our choice of production function. This calculation suggests that the continuation value implied by a multiperiod model should take a similar functional form.

Under the two simplifying assumptions, we have that the transfer to the financial sector is  $T_0 = \theta_0 V(K_1) - N_D$  and there is no probability of default,  $E[1_{def}] = 0$ . Hence, the only choice variable for the government in this case is the tax rate. Appendix A.4 shows that the first-order condition for the government can be written as:

$$\begin{aligned} \frac{d\mathcal{G}}{d\mathcal{T}} + \frac{d\mathcal{L}}{d\mathcal{T}} &= 0, \text{ where} \\ \frac{d\mathcal{G}}{d\mathcal{T}} &= \frac{\partial f(K_0, s_0)}{\partial s_0} (1 - p_{solv}) \frac{ds_0}{dT_0}, \quad \text{and} \\ \frac{d\mathcal{L}}{d\mathcal{T}} &= \theta_0 V'(K_1) \frac{dK_1}{d\mathcal{T}}. \end{aligned} \tag{8}$$

This expresses the first-order condition in terms of the choice of transfer size ( $T_0$ ) and expected tax revenue ( $\mathcal{T}$ ), rather than in terms of the tax rate, and equates the marginal gain and marginal loss of increasing tax revenue.

**Gain From Increased Provision of Financial Services:** The term  $d\mathcal{G}/d\mathcal{T}$  in (8) is the marginal gain to the economy of increasing expected tax revenue. Equations (5) and (6) show that it reflects the wedge between the social and private benefits of an increase in financial services. Since  $ds_0/dT_0 > 0$ , the marginal gain from increasing tax revenue (and hence the transfer) will be large when  $p_{solv}$  is low, that is, when the financial sector is at high risk of insolvency and debt-overhang is significant.

**Under-Investment Loss Due to Taxes:** The term  $d\mathcal{L}/d\mathcal{T}$  in (8) is the marginal under-investment loss to the economy due to a marginal increase in expected tax revenue, which distorts the non-financial sector's incentive to invest. Equation (7) shows that it reflects the size of the tax-induced distortion, which is greater than zero as long as the tax rate is positive. Since  $dK_1/d\mathcal{T} < 0$ , then  $d\mathcal{L}/d\mathcal{T} < 0$ .

**The Optimal Tax Rate and Issuance of Debt:** The following proposition, which describes the solution to the government's problem under assumptions 1 (certainty), 2 (no default) and  $m \geq 2\vartheta$ , is proven in Appendix A.6.

**Proposition 1.** *There is a unique optimal tax rate,  $\hat{\theta}_0$ , which is strictly less than  $\theta_0^{max}$ . Let  $\hat{\mathcal{T}}$  represent the associated tax revenues. Then newly issued sovereign debt has face value  $N_T = \hat{\mathcal{T}} - N_D$  and a price of  $P_0 = 1$ . Moreover,*

1. *The optimal tax rate and revenue are **increasing** in  $L_1$ , the financial sector liabilities, and in  $N_D$ , the outstanding government debt.*

2. The face value of newly issued sovereign debt (the transfer) is **increasing** in the financial sector liabilities  $L_1$ , but **decreasing** in the amount of existing government debt  $N_D$ . Moreover, the gross transfer,  $T_0 + k_A N_D$ , is also **decreasing** in  $N_D$ .
3. If also  $m \leq 2$ , then the optimal tax rate, revenue, and newly issued sovereign debt, are **increasing** in the factor share of the financial sector.

The optimal tax rate is less than  $\theta_0^{max}$  due to the Laffer-curve property of tax revenues. In addition, if there is any debt-overhang (i.e.,  $p_{solv} < 1$ ), then the optimal tax rate will be strictly greater than zero, since at a zero tax rate there is a marginal benefit to having a transfer but no marginal cost.

Consider the three parts of Proposition 1.

For any level of transfer, the marginal gain from the transfer is greater the more severe is the debt-overhang, since a lower probability of solvency increases the distortion in the provision of financial services. Therefore, as (1) and (2) of Proposition 1 state, an increase in  $L_1$ , the financial sector liabilities, leads to a higher tax rate, more tax revenue, and greater issuance of new sovereign debt to fund a larger transfer.

If the level of pre-existing government debt ( $N_D$ ) is increased, there is again a greater marginal gain from the transfer since for any level of tax revenue, the effective transfer ( $T_0$ ) is smaller, and therefore the probability of solvency of the financial sector is lower. As (1) of Proposition 1 states, this pushes the government to increase the optimal tax rate, tax revenue, and *overall* amount of sovereign debt.

However, as (2) of Proposition 1 shows, the rate of increase in total sovereign debt is less than the increase in  $N_D$ . Hence, under the no-default and certainty assumptions, an increase in existing government debt corresponds to a decrease in *newly* issued sovereign debt and a smaller transfer  $T_0$ . The reason for this decrease is that the underinvestment cost of raising additional tax revenues is increasing.<sup>10</sup>

Finally, Proposition 1 shows that, *ceteris paribus*, a larger factor share of the financial sector in aggregate production implies that the government will issue a greater amount of new debt and a larger transfer. Intuitively, if the financial sector's output is a more important input into production, then there will be a greater marginal gain from an increase in the provision of financial services due to the transfer.<sup>11</sup>

---

<sup>10</sup>Later, we show that the possibility of default or the introduction of uncertainty can alter this result.

<sup>11</sup>The factor share is given by  $\vartheta$ . Note, however, that the comparative static is not simply to vary  $\vartheta$ , but to hold total output constant while doing so. Equivalently, we may think about comparing the ratio to total output of our variable of interest while varying the factor share.

### 3.4 Default Under Certainty

Now we allow the government to deviate from the no-default choice of setting  $N_T = \mathcal{T} - N_D$ . Increasing  $N_T$  above this threshold has both an associated cost and benefit. The benefit is that this can increase the transfer to the financial sector. Recall that the transfer  $T_0$  equals  $P_0 N_T$ , where  $P_0 = \max(1, \mathcal{T}/(N_T + N_D))$  is the price of the government bond. The cost is that when  $N_T > \mathcal{T} - N_D$ , the government will not be able to fully cover its obligations. In that case,  $P_0 < 1$  and the government will default, triggering the dead-weight loss of  $D$ .

Hence, the government's decision on how many new bonds to issue,  $N_T$ , splits the decision space into two regions:

1.  $N_T = \mathcal{T} - N_D$  and  $1_{def} = 0$  (No Default)
2.  $N_T > \mathcal{T} - N_D$  and  $1_{def} = 1$  (Default)

As shown in Appendix A.7, if the choice to default is made, then it is optimal for the government to issue an infinite amount of new debt in order to fully dilute existing debt ( $P_0$  becomes 0) and hence capture all tax revenues towards the transfer. The resulting situation is the same as if existing debt  $N_D$  had been set to zero. Therefore, to determine whether defaulting is optimal, the government evaluates whether its objective function for given  $N_D$  and no default exceeds by at least  $D$  (the deadweight default cost) its objective function with  $N_D$  set to zero. Formally, let  $W_{no.def}$  denote the maximum value of the government's objective function conditional on no default,  $W_{def}$  denote the maximum value conditional on default, and  $W = \max(W_{no.def}, W_{def})$ . The following lemma, which is proved in Appendix A.7, characterizes the optimal government action and resulting equilibrium:

**Lemma 4.** *Conditional on default, it is optimal to set  $N_T \rightarrow \infty$  (and hence  $P_0 \rightarrow 0$ ). This implies that  $W_{def} = W_{no.def}|_{N_D=0} - D$ . Moreover, if default is undertaken then (1) the optimal tax rate is lower,  $\hat{\theta}_0^{def} < \hat{\theta}_0^{no.def}$ ; (2) provided that  $k_A N_D < \hat{\mathcal{T}}^{def}$ , the gross transfer is bigger,  $\hat{T}_0^{def} > \hat{T}_0^{no.def} + k_A N_D$ ; and, (3) equilibrium provision of financial services is higher,  $\hat{s}_0^{def} > \hat{s}_0^{no.def}$ .*

Figure 2 displays the optimal default boundary in  $L_1 \times N_D$  space along with the No-Default and Default regions. The following proposition characterizes how a number of factors push the sovereign towards default, or in other words, move it closer to the default boundary.

**Proposition 2.** *Ceteris paribus, the benefit to defaulting is:*

1. **increasing** in the financial sector liabilities  $L_1$  (severity of debt-overhang), the amount of existing government debt  $N_D$ , and in the factor share of the financial sector.
2. **decreasing** in the dead-weight default cost  $D$ , and in the fraction of existing government debt held by the financial sector  $k_A$ .

Appendix A.8 provides the proof. Consider a worsening of the financial sector's health, leading to a decreased provision of financial services. This increases the marginal gain from further government transfer, and, in turn, increases the gain to the sovereign from defaulting. This is represented by a move towards the right in Figure 2, decreasing the distance to the default boundary. A similar kind of result holds if the factor share of financial services is increased, since the marginal gain of further transfer is higher at every level of transfer.

An increase in existing debt implies a bigger spread between the optimal transfer and tax revenue with and without default. Both the extra transfer and decreased underinvestment represent benefits to defaulting. This is represented by a move upwards in Figure 2, again decreasing the distance to the default-boundary.

It is clear that an increase in the deadweight loss raises the threshold for default.

Finally, and importantly, an increase in the fraction of existing sovereign debt held by the financial sector also raises the threshold for default since the act of defaulting, which is aimed at freeing up resources towards the transfer, causes collateral damage to the financial sector balance sheet. From the vantage point of Figure 2, both an increase in  $D$  and  $k$  cause an outward shift in the default boundary.

### 3.4.1 Two-way Feedback

Propositions 1 and 2 indicate that there is a two-way feedback between the solvency situation of the financial sector and of the sovereign. First, by Proposition 1, a severe deterioration in the financial sector's probability of solvency (e.g., an increase in  $L_1$ ) leads to a large expansion in new debt ( $N_T$ ) by the sovereign, as it acts to mitigate the under-provision of financial services. Since the marginal cost of raising the tax revenue ( $d\mathcal{L}/d\mathcal{T}$ ) to fund this debt expansion is increasing, the sovereign is pushed closer to the decision to default (Proposition 2), as well as is its maximum debt capacity (Lemma 3). Hence, a financial sector crisis pushes the sovereign towards distress.

Going in the other direction, by Proposition 1, a distressed sovereign, e.g., one with high existing debt ( $N_D$ ), will have a financial sector with a worse solvency situation. This is because it is very costly for such a sovereign to fund increased debt to make the transfer to



the financial sector. Hence, a more distressed sovereign will tend to correspond to a more distressed financial sector (lower post-transfer  $p_{solv}$ ). Strategically defaulting is an avenue for a distressed sovereign to free debt capacity for additional transfer. However, large holdings of sovereign debt ( $k$ ) by the financial sector mean that taking this avenue simultaneously causes collateral damage to the balance sheet of the financial sector, limiting the benefit from this option (Proposition 2). In this case, a distressed sovereign is further incapacitated in its ability to strengthen the solvency of its financial sector.

### 3.5 Uncertainty, Default, and Pricing

We now introduce uncertainty about future output (i.e., growth) by allowing the variance of  $\tilde{V}(K_1)$  to be nonzero. Instead of a binary default vs. no-default decision, the government now implicitly chooses a continuous probability of default when it sets the tax rate and new debt issuance. In this case, if raising taxes further incurs a large under-investment loss, the government can choose to increase debt issuance while holding the tax rate constant. This dilutes the claim of existing bondholders to tax revenues, thereby generating a larger transfer without inducing further underinvestment. The trade-off is an increase in the government's probability of default and expected dead-weight default loss. In this case, the sovereign effectively 'sacrifices' its own creditworthiness to improve the solvency of the financial sector, leading to a 'spillover' of the financial sector crisis onto the credit risk of the sovereign.

Although  $\theta_0$  and  $N_T$ , are the variables the government directly chooses, it is more enlightening to look at two other variables that map one-to-one to them. The first variable is  $\mathcal{T}$ , which again equals  $\theta_0 V(K_1)$ , the expected tax revenue. The second variable is:

$$H = \frac{N_T + N_D}{\mathcal{T}}$$

In words,  $H$  is the ratio of outstanding debt to expected tax revenue. It is the sovereign's "insolvency ratio", i.e. its ability to cover its total debt at face value. The government's problem (3) then is equivalent to optimally choosing  $\mathcal{T}$  and  $H$ .<sup>12</sup> Note that the no-default and total-default cases under certainty correspond to setting  $H = 1$  and  $H \rightarrow \infty$ , respectively.

To represent uncertainty we write  $\tilde{V}(K_1) = V(K_1)\tilde{R}_V$ , where  $\tilde{R}_V \geq 0$  represents the shock to  $\tilde{V}(K_1)$ . By construction,  $E[\tilde{R}_V] = 1$ . We also assume that the distribution of  $\tilde{R}_V$

---

<sup>12</sup>Formally, the mapping from  $\theta_0$  to  $\mathcal{T}$  is invertible on  $[0, \theta_0^{max}]$  (as before, we can limit our concern to this region) and given  $\mathcal{T}$ , the mapping from  $H$  to  $N_T$  is invertible. Hence, these alternative control variables map uniquely to the original ones on the region of interest.

is independent of the variables  $K_1$ ,  $\theta_0$ , and  $N_T$ .

**Pricing, Default Probability and the Transfer:** Using  $H$  we can easily express the sovereign's bond price,  $P_0$ , and probability of default,  $p_{def}$ , as follows:

$$P_0 = E_0 \left[ \min \left( 1, \frac{\theta_0 \tilde{V}(K_1)}{N_T + N_D} \right) \right] = E_0 \left[ \min \left( 1, \frac{1}{H} \tilde{R}_V \right) \right], \quad (9)$$

$$p_{def} = \text{prob} \left( \theta_0 \tilde{V}(K_1) < N_T + N_D \right) = \text{prob} \left( \tilde{R}_V < H \right). \quad (10)$$

Note that these quantities depend only on  $H$  and do not directly change with  $\mathcal{T}$ . Next, as  $N_T = (\mathcal{T} - N_D/H)H$ , we can express the transfer in terms of  $\mathcal{T}$  and  $H$ :

$$T_0 = N_T P_0 = \left( \mathcal{T} - \frac{N_D}{H} \right) E_0 \left[ \min \left( H, \tilde{R}_V \right) \right]. \quad (11)$$

**The Optimal Probability of Default:** Appendix A.9 and A.10 derive the first-order conditions for  $\mathcal{T}$  and  $H$ , respectively. The first-order condition for  $\mathcal{T}$ , the expected tax revenues, involves the same transfer-underinvestment trade-off as under certainty (adjusted to account for  $H$ ). Varying  $H$ , the sovereign's insolvency ratio, involves a new trade-off. Raising  $H$  increases the transfer by diluting existing bondholders—it raises outstanding debt but without increasing expected tax revenue. This captures a greater fraction of tax revenues towards the transfer but raises the sovereign's probability of default.

The top panel of Figure 3 illustrates the marginal gain (solid line) and loss (dashed line) incurred by increasing  $H$  for a fixed level of  $\mathcal{T}$ .<sup>13</sup> The marginal cost of an increase in  $H$  is the rise in expected dead-weight default cost. This is shown by the dashed green line in Figure 3. Figure 3 indicates that (with  $\mathcal{T}$  held constant) there are two potential candidates for the optimal choice of  $H$ . The first is the value of  $H$  at which the gain and loss curves intersect. The second is to let  $H \rightarrow \infty$ , representing a total default and full dilution of existing bondholders. The bottom panel of Figure 3 plots the corresponding value of the government's objective as a function of  $H$ . The plot shows that for the configuration displayed, a relatively small value of  $H$  achieves the optimum, which is at the intersection of the gain and loss curves in the top panel. As this optimal  $H$  is beyond the left end of the support of  $\tilde{R}_V$  (which is the origin in the figure), it corresponds to an optimal non-zero

<sup>13</sup>To generate the plots, we need to assume a specific distribution for uncertainty. For simplicity, we let  $\tilde{R}_V$  have a uniform distribution.

probability of default. Note that beyond the upper end of the support of  $\tilde{R}_V$ , the objective function again rises in  $H$ , because once debt issuance is large enough that default is certain, it is optimal for the government to fully dilute existing bondholders to obtain the largest possible transfer. Finally, the dash-dot curves in Figure 3 show a case with an increase in  $L_1$  (more severe debt-overhang in the financial sector) relative to the solid lines.

### 3.5.1 Comparative Statics Under Uncertainty

The government jointly chooses  $\mathcal{T}$  and  $H$  in an optimal way by comparing the relative marginal cost and benefit of adjusting each quantity. When the marginal benefit of additional transfer is large, but the marginal underinvestment loss due to taxation is already high, the government will optimally begin to ‘sacrifice’ its own creditworthiness to generate additional transfer. The following proposition characterizes how different factors impact  $\hat{H}$  and  $\hat{\mathcal{T}}$ , the government’s optimal choices of  $H$  and  $\mathcal{T}$  in equilibrium:

**Proposition 3.** *If  $(\hat{\mathcal{T}}, \hat{H})$  is an interior solution to the government’s problem on a region of the parameter space, then  $\hat{H}$  is **increasing** in  $L_1$ , in  $N_D$  and in  $\vartheta$ , and **decreasing** in  $D$ . Furthermore,  $\hat{\mathcal{T}}$  is also increasing in  $L_1$ .*

Figure 4 plots comparative statics of the equilibrium (optimal) values of  $\mathcal{T}$ ,  $H$ ,  $T_0$ , and  $P_0$  as  $L_1$  and  $N_D$  are varied. The discontinuities that appears in the plots, as indicated by the dotted lines, represent the point at which total default becomes optimal.

The top panel of Figure 4 varies  $L_1$ . It shows that  $\mathcal{T}$  increases monotonically in  $L_1$ , up to the point where the sovereign chooses total default. The corresponding plot for  $H$  tells a different story. For low levels of  $L_1$ ,  $H$  is held constant at a low value. This value corresponds to the lower end of the support of  $\tilde{R}_V$ , so the probability of sovereign default remains 0. Correspondingly, the plot shows that in this range,  $P_0$  remains fully valued at 1. For sufficiently high  $L_1$  (e.g., financial crisis), the government chooses to increase  $H$ . It ‘sacrifices’ its own creditworthiness in order to achieve a larger transfer. The increase in the transfer is apparent in the subplot for  $T_0$ , while the damage to the sovereign’s creditworthiness is apparent in the plot for  $P_0$ , which begins to decrease once  $H$  begins to rise.<sup>14</sup>

The plots also show that when the financial sector’s situation is severe enough ( $L_1$  is large), the optimal government response can be a total default. The outcome of a total default is illustrated in the plots at the point of the dotted line. As in the certainty case,

---

<sup>14</sup>Note that the transfer increases more rapidly in  $L_1$  once  $H$  begins to increase. This occurs because higher  $H$  means a greater proportion of expected tax revenue is captured towards the transfer.

total default fully dilutes existing bondholders, freeing extra capacity for the sovereign to generate the transfer. As indicated in the plots, this leads to a jump up in  $T_0$  and a jump down in  $\mathcal{T}$ . At the same time,  $P_0$  drops to 0.

The bottom panel of Figure 4 shows the comparative statics for  $N_D$ . It is apparent that for low levels of legacy debt the sovereign keeps  $H$  constant at the low end of its support, so there is no probability of default and  $P_0$  remains at 1. For these values of  $N_D$ , the government funds the transfer exclusively through increases in tax revenues. Note that in this range the transfer is decreasing in  $N_D$ , similar to the case of certainty. Once  $N_D$  is sufficiently high, the underinvestment costs of increasing tax revenue become so high that the sovereign begins to increase  $H$  to fund the transfer. Consequently, the probability of default rises and  $P_0$  begins to decrease, as shown in the plot. Interestingly, in this range the combination of increased  $H$  and  $\mathcal{T}$  imply that the transfer is actually *increasing* in  $N_D$ . The reason for this is that for large  $N_D$ , the dilution of existing bondholders is an effective channel for increasing the transfer. Moreover, as the plots show, at high enough  $N_D$ , total default becomes optimal.

### 3.6 Government ‘Guarantees’

Explicit government guarantees of financial sector debt have been a part of a number of countries’ financial sector bailouts, notably Ireland. Moreover, it has been common for sovereigns to step in to prevent the liquidation of banks by guaranteeing their debt, which strongly suggests that there is an implicit ‘safety net’.<sup>15</sup>

In this section, we add to the model a simple notion of a government guarantee of financial sector debt. We do this for two reasons. First, guarantees are a measure that serves to prevent liquidation of the financial sector by debtholders, which is a necessary pre-condition for increasing the provision of financial services. Second, guarantees are rather unique in that, by construction, their benefit is targeted at debt holders and not equity holders. This unique feature is important in helping us identify empirically a main implication of our model, that there is direct feedback between sovereign and financial sector credit risk.

In the interest of simplicity, and since debt-overhang alleviation is the central feature of bailouts in the model, we do not explore the feedback of the guarantees on the transfer and taxation decisions analyzed above. Instead, we simply set the stage for the implications of the guarantees for our empirical strategy.

---

<sup>15</sup>The fallout from the failure of Lehman brothers and the apparent desire to prevent a repeat of this experience has strongly reinforced this view.

### 3.6.1 Avoiding Liquidation

We model debtholders as potentially liquidating (or inducing a run on) the financial sector if they are required to incur losses in case of financial sector default. To prevent debtholders from liquidating, the government ‘guarantees’ their debt. That is, it pledges to bondholders  $L_1 - \tilde{A}_1 - T_0$  from tax revenues in case of insolvency. The guarantee is pari-passu with other claims on tax revenue. Hence, the guarantee has the same credit risk as other claims on the sovereign. In fact, the guarantee is just equivalent to a claim that issues  $L_1 - \tilde{A}_1 - T_0$  new government bonds to debt holders in case of insolvency.

Note that this claim accrues exclusively to debtholders and not to equityholders. This differentiates it from general assets of the financial sector, such as the asset paying  $\tilde{A}_1$  or the transfer,  $T_0$ . Importantly, a change in the value of general assets of the firm changes the value of equity and debt in a certain proportion, while a change in the value of the guarantee changes the value of debt but not the value of equity. This implies that, if there are guarantees, the change in equity value will not be sufficient for determining the change in debt value. The following proposition gives a formal statement of this, derived under a uniform distribution for  $\tilde{A}_1$  (same as used above to generate the figures).

**Proposition 4.** *Let  $D$  be the value of debt,  $E$  the value of equity, and  $\tilde{A}_1 \sim U[A_{min}, A_{max}]$ . In the absence of a guarantee, the return on equity is sufficient for knowing the return on debt. In contrast, in the presence of a guarantee, the return on debt is a bivariate function of both the return on equity and the return on the sovereign bond price.*

This bivariate dependence is approximated by the following relation:

$$\frac{dD}{D} \approx \frac{(1 - p_{solv})(1 - P_0)}{p_{solv}} \frac{E}{D} \frac{dE}{E} + \frac{(1 - p_{solv})^2 (A_{max} - A_{min})}{2} \frac{P_0}{D} \frac{dP_0}{P_0}, \quad (12)$$

which is derived in the Appendix. The term involving the equity return ( $\frac{dE}{E}$ ) captures the impact on the debt value of any changes in the value of the general pool of assets of the firm, including changes in the firm’s expected future profits. This type of result goes back to Merton (1974), where the changes in both the debt and equity value reflect the change in the total value of the firm. In the presence of a guarantee, there is an additional component, which picks up the change in the value of debt coming from changes in the value of the government guarantee. The change in value of the guarantee, which reflects variation in the credit risk of the sovereign ( $\frac{dP_0}{P_0}$ ), is concentrated primarily with debt and therefore not

captured adequately by the return on equity.<sup>16</sup>

### 3.6.2 Two-way Feedback Revisited

Proposition 3 and Figure 4 show that with uncertainty about future output, the ‘spillover’ of the financial sector crisis onto the sovereign takes the form of a higher insolvency ratio  $H$ , which is reflected in a lower sovereign bond price (and higher CDS rate).

The creditworthiness of the sovereign also feeds back directly onto the credit risk of the financial sector. Governments that have a higher level of legacy debt ( $N_D$ ) generate smaller transfers and so the health of their financial sectors will be relatively weaker post-transfer (lower post-transfer  $p_{solv}$ ). Furthermore, once a bailout pushes the government to increase its insolvency ratio  $H$ , its debt becomes risky and propagates through to banks negative sovereign shocks (e.g., shocks to growth and tax revenue  $\tilde{R}_V$ ) via changes in the value of their sovereign debt exposure—the transfer, holdings of legacy government debt, and government guarantees. This feedback implies a post-bailout increase in co-movement between sovereign and financial sector credit risk.

## 4 Empirics

In this section we present empirical evidence in favor of the main arguments formalized in our model: (1) bank bailouts reduced financial sector credit risk but were a key factor in triggering the rise in sovereign credit risk of the developed countries, and (2) there is a two-way feedback between the credit risk of the sovereign and the financial sector.

The setting for our empirical analysis is the financial crisis of 2007-10. We divide the crisis into three separate periods relative to the bailouts: *pre*, *around*, and *after*. The pre-bailout period, which culminated in Lehman Brother’s bankruptcy, saw a severe deterioration in banks’ balance sheets, a substantial rise in the credit risk of financial firms, and a significant loss in the market value of bank equity. This negative shock generated substantial debt overhang in the financial sector and significantly increased the likelihood of failure of, or

---

<sup>16</sup>Note that there is theoretically also an indirect feedback of sovereign credit risk on financial sector credit risk. This is because the guarantee represents additional (state-contingent) debt issuance by the sovereign, which raises expected default costs of the sovereign and potentially reduces the size of the transfer to the financial sector. As mentioned above, to maintain simplicity we will not incorporate the impact of the guarantee on the government’s optimal choice of tax revenue or debt issuance. Instead, we will mainly use the above result to motivate part of our empirical work.

runs on, financial institutions. We interpret this as setting the stage for the initial time period in the model, and the bank bailouts as the sovereign’s response, per the model.

We present our empirical results in two parts. The first part focuses on point (1). We present evidence that the bailouts transmitted risk from the banks to the sovereigns and triggered a rise in sovereign credit risk across a broad cross-section of developed countries. We then confirm a prediction of the model by documenting the post-bailout emergence of a positive relationship between sovereign credit risk and government debt-to-gdp ratios. We also analyze the ability of the pre-bailout credit risk of the financial sector and the pre-bailout government debt-to-gdp ratio to predict post-bailout sovereign credit risk. This relationship is predicted by the model and is supportive of the argument that the bailouts led to the emergence of sovereign credit risk in developed countries.

The second part of our analysis focuses on point (2) by testing for the sovereign-bank two-way feedback. We use a broad panel of bank and sovereign CDS data to carry out tests that establish this channel and show that it is quantitatively important. A significant challenge in demonstrating *direct* sovereign-bank feedback is the concern that another (unobserved) factor directly affects both bank and sovereign credit risk, giving rise to co-movement between them even in the absence of any direct feedback. We address these concerns by utilizing a particularly useful feature of government ‘guarantees’—that they are targeted specifically at bank debt holders. This allows us to control for bank fundamentals using equity returns and establish the direct sovereign-bank feedback.

We also gather data on the sovereign bond holdings of European banks that were released after the stress tests conducted in the first half of 2010. Using these data we show that bank holdings of foreign sovereign bonds have information about how sovereign credit risk affects a bank’s credit risk. This result provides further evidence of a direct sovereign-to-bank feedback because we control for country-specific macroeconomic changes by using the change in value of foreign (rather than home) sovereign bonds.

We next describe the data construction and provide some summary statistics.

## 4.1 Data and Summary Statistics

We use Bankscope to identify all banks headquartered in Western Europe, the United States, and Australia with more than \$50 billion in assets as of the end of fiscal year 2006. We choose this sample because smaller banks and banks outside these countries usually do not have traded CDS. We then search for CDS in the database Datastream. We find CDS for 99

banks and match CDS to bank characteristics from Bankscope. Next, we search for equity returns using Datastream. We find equity returns for 62 banks and match returns to CDS and bank characteristics. Finally, we match these data to sovereign CDS (based on bank headquarters) and OECD Economic Outlook data on public debt.

Panel A of Table 1 presents summary statistics for all banks with CDS prices. As of July 2007, the average bank had assets of \$589.3 billion and equity of \$26.8 billion. The average equity ratio was 5.1% and the average Tier 1 ratio was 8.5%. The average bank CDS was 21.8 bps and the average sovereign CDS (if available as of July 2007) was 6.6 bps.

Panel B of Table 1 present summary statistics of weekly changes in bank CDS and sovereign CDS for the main bailout periods. We drop all observations with zero changes in bank CDS or sovereign CDS to avoid stale data. All results presented below are robust to including the dropped observations. Before the bank bailouts, the average bank CDS was 93.2 bps. The average sovereign CDS was 13.5 bps. The low level of sovereign credit risk suggests that financial market participants did not anticipate large-scale bank bailouts prior to September 2008.

In the bailout period, we see a significant rise in both bank and credit risk with average bank and sovereign CDS of 288.6 bps and 39.3 bps, respectively. As we discuss below, a substantial part of the increase in bank credit risk was triggered by the Lehman bankruptcy. Bank equity values declined sharply during this period with a negative weekly return of 6.7%.

In the post-bailout period, average bank and sovereign CDS were 188.7 and 108.5 bps, respectively. These CDS levels are suggestive of a significant transfer of financial sector credit risk on sovereign balance sheets. We also find significant variation in sovereign CDS with a standard deviation of weekly changes of 11.3%. This evidence suggests the emergence of significant sovereign credit risk after the bank bailouts.

## 4.2 The Sovereign Risk Trigger

### 4.2.1 Bank and Sovereign CDS

The first bank bailout announcement in Western Europe was on September 30, 2008 in Ireland. We define the *pre-bailout* period as starting on January 1, 2007 and ending on September 26, 2008. We start the period in January 2007 to include the increase in bank credit risk because of the financial crisis. Note that the pre-bailout period includes the bankruptcy of Lehman Brothers on September 15, 2008 and the period immediately after-



wards, so that it includes the immediate effect of Lehman's bankruptcy on other banks. Hence, the pre-bailout period captures both the prolonged increase in bank credit risk during 2007-2008 and the post-Lehman spike that occurs before the bank bailouts. To examine bank and sovereign credit risk in this period, we analyze the country-level change in sovereign and bank CDS. For each country, we compute the change in bank CDS as the unweighted average of all banks with traded CDS.

Figure 5 summarizes the results for the pre-bailout period. For each country, the first column depicts the change in sovereign CDS and the second column depicts the change in bank CDS over the pre-bailout period. The figure shows that there is a large increase in bank CDS during this period. For example, the average bank CDS in Ireland increases by 300 bps. However, there is almost no change in sovereign CDS. Overall, the figure shows that the credit risk of the financial sector was greatly increased over the pre-bailout period but that there was little impact on sovereign credit risk.<sup>17</sup>

Within one month after the Irish bailout, almost every Western European country announced a bank bailout. The bailouts typically consisted of asset purchase programs, debt guarantees, and equity injections or some combination therefore. The programs were substantial with up-front government financing of up to 20% of GDP. Several countries made more than one announcement during this period. As noted above, the first country to make a formal announcement was Ireland on September 30, 2010. Many other countries soon followed Ireland's example, in part to offset outflows from their own financial sectors to newly secured financial sectors. As a result, the bank bailout announcements were not truly independent since sovereigns partly reacted to other sovereigns' announcements. We therefore define the bailout period as the one-month period in which most bank bailouts were first announced.

Figure 6 plots the average change in bank CDS and sovereign CDS during the bailout period. For most countries, bank CDS significantly decreased over this one-month period. For example, the average bank CDS in Ireland decreased by about 200 bps. At the same time, there is a significant increase in sovereign CDS. For example, the sovereign CDS of Ireland increased by about 50 bps. Most other countries exhibit a similar pattern with

---

<sup>17</sup>We note that some investors may have expected bank bailouts even before the first official announcement on September 30, 2008. Such an expectation would reduce the observed increase in bank CDS and shift forward in time the rise in sovereign CDS. To the extent that investors held such expectations prior to September 30, 2008, they can explain the small rise in sovereign CDS that occurs late in the pre-bailout period. However, the fact that the impact in this period is so small quantitatively suggest that the bank bailouts were a surprise to the majority of investors.

decreasing bank CDS and increasing sovereign CDS.

The appearance of this striking pattern across a broad cross-section of countries is directly in line with the predictions of our model. It shows that the sovereigns responded to the distress in the financial sector with the bailouts, achieving a substantial reduction in banks' credit risk. However, in accordance with our model, this caused a contemporaneous, immediate increase in the sovereigns' credit risk.

Next, we examine the period after the bailouts. We define the post-bailout period as beginning after the end of the bank bailouts and ending in March 2010. We choose March 2010 because this is the date for which the European bank stress data results were released but prior to large-scale interventions by the European Central Bank. The qualitative results are robust to using later cut-off dates.

Figure 7 plots the change in bank CDS and sovereign CDS over the post-bailout period. We find that both sovereign CDS and bank CDS increased across most countries. Moreover, bank CDS and sovereign CDS move together after the bank bailouts. This suggests that they are tied together and potentially feedback on each other as suggested by our model and as we further explore below.

#### **4.2.2 Debt Ratios, Financial Distress and Sovereign CDS**

Our model predicts that the increase in sovereign credit risk upon bailouts should depend on the pre-bailout debt of the sovereign and the pre-bailout level of financial sector distress. The model also suggests that there should be a positive relationship between sovereign credit risk and measures of government debt-to-gdp after the bailout even if no such relationship appears beforehand.

Figure 8 shows the relationship between debt-to-gdp ratio and sovereign CDS across countries. The upper panel plots the relationship before the bailouts. The panel shows almost no correlation between the two variables. The lower panel plots the relationship after the bank bailouts. The panel shows a strong and positive relationship between the two variables. These figures are highly suggestive of a link between public debt and sovereign credit risk because of the bank bailouts.

To test this relationship more formally, we use data on sovereign CDS, financial sector distress, and government debt-to-gdp ratios. We measure pre-bailout financial sector distress at the country level by averaging bank CDS on September 22, 2008. We choose this date midway between Lehman's bankruptcy and the first bailout announcement. We measure the government debt-to-gdp ratio as the government gross liabilities as a percentage of gdp in

the year before the bailouts. For the post-bailout date we again choose March 31, 2010, the reporting date for the European bank stress tests. We estimate the following regression:

$$y_i = \alpha + \beta(\text{Pre-Bailout Debt}_i) + \gamma \log(\text{Financial Sector Distress}_i) + \varepsilon_i$$

where the outcome variable  $y_i$  is either the natural logarithm of sovereign CDS or the debt-to-gdp ratio of country  $i$ .

Table 2 presents the result of our analysis. We first focus on the post-bailout results. Column (3) finds that a 1% increase in the pre-bailout debt-to-gdp ratio leads to a 1.5% increase in sovereign CDS post-bailout.<sup>18</sup> Column (4) shows that a 1% increase in pre-bailout financial sector distress increases post-bailout sovereign CDS by 0.965%. The coefficient on debt-to-gdp decreases slightly but remains marginally significant. The R-squared of the regression is close to 50%. These results suggest that pre-bailout financial sector distress and sovereign's debt-to-gdp ratio are highly predictive of post-bailout sovereign credit risk.

In contrast, Column (1) of Table 2 shows that in the pre-bailout period there is only a very weak relationship between debt-to-gdp and sovereign CDS. The coefficient is small and statistically insignificant. Column (2) shows that the coefficient on financial sector distress in the pre-bailout period is also statistically insignificant.

From these results we can see that there emerged a relationship between debt-to-gdp and sovereign credit risk that was not present beforehand. Note, moreover, that the emergence of this relationship coincides with an overall rise in sovereign debt ratios. In the context of our model, the sovereigns have increased debt-to-gdp ratios into the region where dilution of existing debt occurs and there is a negative relationship between debt ratios and the government bond price (see Figure 4).

Column (5) examines the ability of pre-bailout financial sector distress to predict the change in government debt-to-gdp from the pre-bailout to the post-bailout period. Consistent with the model, we find that financial sector distress is positively related to the increase in debt-to-gdp. The coefficient is positive and marginally statistically significant. Column (6) shows that consistent with the model's predictions, post-bailout debt-to-gdp is predicted by pre-bailout debt-to-gdp and pre-bailout financial sector distress. Both coefficients are statis-

---

<sup>18</sup>We make note of two points. First, the model predicts that  $H$  determines the level of sovereign CDS. However, the debt-to-gdp ratio corresponds to  $\theta_0 H$  in the model rather than simply  $H$ . Nevertheless, the prediction of the model carries over to  $\theta_0 H$  since  $\theta_0$  is increasing in financial sector distress. Second, debt-to-gdp ratios are an imperfect proxy for  $\theta_0 H$  because  $H$  takes into account any future issuance of debt to pay for current obligations related to the bailouts, whereas debt-to-gdp ratios are lagging. We can address this to some extent by using leading debt-to-gdp.

tically significant and together the two variables explain 84% of the variation in post-bailout debt-to-gdp.

### 4.3 The Sovereign-Bank Feedback

This section analyzes the two-way feedback between sovereign and bank sector credit risk. Once the sovereign opens itself up to credit risk due to bailouts, the price of its debt becomes sensitive to macroeconomic shocks. Moreover, our model indicates that subsequent changes in the sovereign’s credit risk should impact the financial sector’s credit risk through three channels: (i) ongoing bailout payments and subsidies,<sup>19</sup> (ii) direct holdings of government debt, and (iii) explicit and implicit government guarantees. In our empirical analysis, we estimate the aggregate effect of these three channels.

We start by estimating the following relationship in the post-bailout period:

$$\Delta \log(\text{Bank CDS}_{ijt}) = \alpha + \beta \Delta \log(\text{Sovereign CDS}_{jt}) + \varepsilon_{ijt}$$

where  $\Delta \log(\text{Bank CDS}_{ijt})$  is the change in the log CDS of bank  $i$  headquartered in country  $j$  from time  $t$  to time  $t - 1$  and  $\Delta \log(\text{Sovereign CDS}_{jt})$  is the change in the log Sovereign CDS of country  $j$  from time  $t$  to time  $t - 1$ . At the weekly frequency, in the post-bailout period the estimate of  $\beta$  is 0.47 and highly statistically significant. This means that a 10% increase in sovereign CDS is associated with a 4.7% increase in bank CDS. This result suggests that sovereign and bank CDS exhibit a strong comovement, which is consistent with direct sovereign-to-bank feedback.

However, an obvious concern is that there is another (unobserved) factor that affects both bank and sovereign credit risk. Such a factor could explain the co-movement without there necessarily being an underlying *direct* channel between sovereign and bank credit risk. More specifically, we interpret changes in sovereign credit risk as changes in expectations about macroeconomic fundamentals, such as employment, growth, and productivity. These fundamentals also have a direct effect on the value of bank assets such as mortgages or bank loans. Hence, changes in macroeconomic conditions may generate a correlation between sovereign and bank credit risk even in the absence of the direct feedback mechanism.

---

<sup>19</sup>While we model the bailout as happening in one stage, in practice bailouts may occur in multiple steps. This may occur when early efforts are deemed to be insufficient. As with the one-stage bailout in our model, the sovereign’s creditworthiness is important in determining the potential for and magnitude of future bailout steps. This presents another, dynamic channel through which changes in sovereign creditworthiness impact both financial sector debt and equity values.

Therefore, establishing that there is a direct feedback between sovereign and financial sector credit risk is a significant empirical challenge.

We use several strategies to address this concern. Our first strategy is to include three sets of controls. First, we add controls that capture market-wide changes that affect both bank and sovereign risk directly. Our market-wide controls are a CDS-market index and a measure of aggregate volatility. Our CDS market index is the iTraxx Europe index, which is comprised of 125 of the most liquid CDS names referencing European investment grade credits. The CDS market index captures market-wide variation in CDS rates caused by changes in fundamental credit risk, liquidity, and CDS-market specific shocks.<sup>20</sup> For the volatility index we follow the empirical literature and use a VIX-like index, the VDAX, which is the German counterpart to the VIX index for the S&P 500. This captures changes in aggregate volatility, which is an important factor in the pricing of credit risk. Second, we include weekly fixed effects. The fixed effects captures (unobserved) variation that is common across all banks. Third, we include bank-specific coefficients on all the control variables and bank fixed effects. This accommodates potential non-linearities in the estimated relationships.

We implement this approach by estimating the following regression:

$$\Delta \log(\text{Bank CDS}_{ijt}) = \alpha_i + \delta_t + \beta \Delta \log(\text{Sovereign CDS}_{jt}) + \gamma \Delta X_{ijt} + \varepsilon_{ijt}$$

where  $\Delta X_{ijt}$  are the changes in the control variables from time  $t$  to time  $t - 1$ ,  $\delta_t$  are weekly fixed effects, and  $\alpha_i$  are bank fixed-effects.

Table 3 shows the results for the pre-, around, and post-bailout period. For each period there are three columns of results. The left column reports the coefficient after including the market-wide control variables. The middle column adds the weekly fixed effects. The right column adds bank fixed effects and bank-specific coefficients on controls.

Our main focus is on testing for the sovereign-bank feedback, so we examine the post-bailout results first. Column (7) shows that  $\beta$  is positive, as expected, and highly statistically significant. The magnitude is also economically important, implying that an increase in sovereign CDS of 10% translates into a 2.21% increase in bank CDS. The control coefficients are both statistically significant and the signs are as expected; an increase in aggregate CDS levels or aggregate volatility is associated with a rise in bank CDS. Altogether, the variables

---

<sup>20</sup>Collin-Dufresne, Goldstein, and Martin (2001) find that a substantial part of the variation in corporate credit spread changes is driven by a single factor that is independent of changes in risk factors or measures of liquidity. They therefore conclude that this variation represents ‘local supply/demand shocks’ in the corporate bond market.

explain 33.8% of the variation in weekly bank CDS.

Column (8) adds the weekly fixed effects. The coefficient on sovereign CDS decreases but remains highly statistically significant. The decrease is not surprising, as time fixed effects represent a rich set of controls. The weekly fixed effects are collinear with the market-wide control variables; therefore, we do not estimate coefficients on the market-wide controls. There is an increase in the R-squared of about 7.6% over column (7), indicating that most of the unobserved market-wide variation was already captured by the market-wide controls.

Column (9) shows that the coefficient on sovereign CDS is essentially unchanged and remains highly statistically significant after adding bank-specific coefficients on the control variables. Given the flexibility of this specification, we interpret the coefficients on sovereign CDS as robust evidence in favor of direct sovereign-to-bank feedback.

Comparing these results with those for the around-bailout period in columns (4)-(6) shows interesting differences. For the around-bailout period, the coefficient on sovereign CDS is *negative* after controlling for week fixed effects. In other words, in the around-bailout period an increase in sovereign CDS is associated with a *decrease* in bank CDS. This is very much consistent with the evidence presented above that the sovereigns took onto themselves credit risk from their financial sectors during this phase. As shown in Column (6), the coefficient is large and statistically significant with a 10% increase in sovereign CDS leading to 12.9% decrease in bank CDS.

Columns (1)-(3) show the results for the pre-bailout period. They show small coefficients on sovereign CDS that are indistinguishable from zero. As expected, in the pre-bailout period there is no evidence for sovereign-bank feedbacks. In contrast, the CDS market control coefficient is significant and has a large magnitude, similar to the results for the other periods.

We also provide a non-parametric illustration of this result. We add interactions of year-month fixed-effects and sovereign CDS to the regression model describe above (including all controls). Figure 9 plots the three-month moving average of the coefficients on the interactions. As shown in the figure, there is no correlation between bank and sovereign CDS in the pre-bailout period, the relationship is negative during the bailout period, and positive throughout the entire post-bailout period. This result lends further support to our analysis of three distinct bailout periods.

### 4.3.1 Controlling for Bank Fundamentals

The results above establish that there is a strong two-way sovereign-bank feedback. However, there may remain a concern that our strategy to this point does not control for country-specific macroeconomic shocks that affect both sovereign and credit risk. For example, a negative shock to expected growth will decrease the value of banks' assets or future earnings power, while at the same time reducing national output. This will raise bank and sovereign CDS even in the absence of a direct feedback between them. This shock may not be fully captured by our market-wide controls if it has a heterogenous impact across countries.

We address this concern employing a strategy that utilizes a particularly useful feature of bank bailouts. Specifically, most bailouts were partly structured in the form of government 'guarantees', which are targeted specifically at bank debt holders. This implies that sovereign-specific shocks should have a disproportionate impact on debt holders because, in addition to changing the value of bank assets, such shocks change the value of government 'guarantees' (implicit or explicit). Therefore, to establish whether there is direct sovereign-to-bank feedback, we can test if sovereign CDS is a determinant of bank CDS even after we control for the impact of shocks to bank fundamentals.

Our empirical strategy for dealing with this concern is motivated by the model. Our guarantees model (Section 3.6) shows that bank equity returns are sufficient for determining changes in bank CDS in the absence of government 'guarantees'.<sup>21</sup> This implies that once we control for bank equity returns we should *not* find that changes in sovereign CDS have any further explanatory power for changes in bank CDS. Indeed, a-priori it seems that even if there are direct sovereign-to-bank feedback channels, their impact may be subsumed into an equity control, making it difficult to document their existence. On the other hand, if one finds that sovereign CDS *does* have further explanatory power for bank CDS beyond equity returns, then this is strongly supportive of a sovereign-to-bank feedback channel. Proposition 4 shows that 'guarantees' present a source for such a potential finding because they discriminate precisely in favor of debtholders. In the presence of 'guarantees', a projection of changes in bank CDS that controls for equity returns should still find a (positive) exposure on changes in sovereign CDS.

We therefore augment the regression with banks' weekly equity returns. The estimates are shown in Table 4. The structure is similar to Table 3. Columns (7)-(9) show that in

---

<sup>21</sup>This result is in fact quite general. It holds in models of defaultable bond pricing that build on the canonical model of Merton (1974), where stock returns contain all information about changes in bank asset values and therefore can (locally) capture all variation in the price of debt.

the post-bailout period the coefficient on sovereign CDS survives and is highly statistically significant. As shown in columns (7) and (8), although the bank stock return coefficient is highly statistically significant and possesses the expected negative sign, its inclusion has little impact on the magnitude of the sovereign CDS coefficient. Column (9) includes bank-specific coefficients on bank stock returns. The results show that the coefficient on sovereign CDS decreases somewhat but remains highly significant.

We note that the coefficients in Column (7) to (9) are slightly smaller than the comparable coefficients in Table 3. This is consistent with small, positive benefits of bank bailouts to bank equity holders.

For the bailout and pre-bailout periods, the results are quite similar to those in Table 3. As shown in columns (1) to (6), we again find a negative coefficient on sovereign CDS in the bailout period and an essentially zero coefficient in the pre-bailout period.

### 4.3.2 Bank-level Heterogeneity

To analyze further the sovereign-bank feedback, we also examine whether heterogeneity in bank characteristics affects banks' sensitivity to changes in sovereign CDS. To this end, we estimate the coefficient on an interaction term of changes in sovereign CDS and a bank's Tier 1 capital ratio. The Tier 1 capital ratio is commonly used in the banking industry as a proxy for a bank's probability of solvency. This specification is motivated by the model. Our guarantees model suggests that we should find that the magnitude of the coefficient on changes in sovereign CDS is decreasing in banks' Tier 1 ratios. Intuitively, the impact of changes in the value of government guarantees is stronger for less well-capitalized banks.

Table 5 reports the results. The coefficient of interest is the interaction term. For the post-bailout period, the negative estimates for the interaction term indicate that banks with higher Tier 1 ratios were less sensitive to variation in sovereign CDS rates. Although the estimates are negative in columns (7) to (9), only column (9), which includes the full set of controls is statistically significant.

The results in the bailout period are surprising. Similar to the post-bailout period, the coefficient on the interaction term is negative. This implies that well-capitalized banks experienced a larger CDS decrease relative to poorly capitalized banks during the bailout period.<sup>22</sup> In the pre-bailout period, the interaction term is positive but small and statistically insignificant.

---

<sup>22</sup>This might perhaps reflect that bailout packages partly attempted to "pool" the risks of banks in the economy.



### 4.3.3 The Impact on Equity Value

For the purposes of establishing the existence of a two-way feedback we have mainly focused on changes in bank CDS. It is also interesting to look at the impact of bailouts on bank stock returns. From the viewpoint of the model, bank stock returns should reflect changes in sovereign credit risk due to their impact on the value of continuing bailout payments and banks' holdings of government bonds. To that end, we estimate the following regression:

$$\text{Bank Stock Return}_{ijt} = \alpha_i + \delta_t + \beta \Delta \log(\text{Sovereign CDS}_{jt}) + \gamma \Delta X_{ijt} + \varepsilon_{ijt}$$

where  $\text{Bank Stock Return}_{ijt}$  is the stock return of bank  $i$  headquartered in country  $j$  from time  $t$  to time  $t - 1$ . We use the same control variables as in Table 4.

Table 6 presents the results. Columns (7) to (9) show that in the post-bailout period an increase in sovereign CDS is associated with a decrease in bank stock returns. This result is robust to the inclusion of the full set of controls. Note also that the coefficients on the controls have the expected signs and are significant.

During the bailout period, the coefficient on sovereign CDS is not distinguishable from zero. The point estimate is positive in columns (5) and (6), but is not statistically significant. Still, across the board, the point estimates are clearly higher than for the post-bailout period, which is consistent with the idea that equity holders benefitted from bank bailouts. One potential offsetting effect on this result is that in some countries the benefits of bailouts to equity holders were offset by charges (or expectations of charges) levied by the government.

Columns (1) to (3) show that as before, the coefficient on sovereign CDS in the pre-bailout period is essentially zero.

### 4.3.4 Robustness

We conduct several other tests to ensure the robustness of our results. Our main regressions are estimated at the weekly level. Estimation at the weekly level allows us to smooth out measurement error that can bias our results. This is important in our context because we are first differencing our data, which magnifies any existing measurement error. However, by using weekly level we may also allow for more (unobserved) omitted variables that can affect our results.

We therefore revisit our evidence in Tables 3 and 4 and estimate all regressions at the daily level. We replace week fixed effects with day fixed effects. Panel A of Table 7 presents the results without controlling for equity (Table 3) and Panel B presents the results with

controlling for equity (Table 4). We find qualitatively similar results to our main specifications: there is no relationship in the pre-bailout period, a statistically significant and negative relationship during the bailout period, and a statistically significant and positive relationship during the post-bailout period. The estimates are on average about one third smaller than the estimates with weekly data, which is consistent with some measurement error in the first-differenced daily data.

We also note that our results are estimated using changes of log CDS. We choose this specification because log changes are robust to the inclusion of outliers. Alternatively, we can also estimate our results using arithmetic CDS changes. We find that our main results are robust to using arithmetic CDS changes instead of log CDS changes. The only difference is that the results with arithmetic changes are more sensitive to the inclusion of time fixed-effects. This is not surprising because without time fixed-effects we rely on changes in the CDS market index and the VDAX index to capture changes in general market conditions. Given that these indices are necessarily expressed in percentage terms, this assumption is less likely to hold for arithmetic changes relative to log changes.<sup>23</sup>

#### 4.4 European Bank Stress Test Analysis

As a final part of our analysis, we use data on the sovereign bond holdings of European banks. These data were released as part of the European bank stress tests, which were conducted in the first half of 2010. The data provide a view of a bank's bond holdings of both its own government bonds and those of other European countries.

We first describe the data and provide summary statistics. We collect the stress test data from the websites of national bank regulators in Europe. The data consists of bank characteristics and holdings of European sovereign bonds. A total of 91 banks participated in the bank stress tests. These banks represent about 70 percent of bank assets in Europe. For all banks, we search for CDS prices in the database Datastream. Using bank names, we match 51 banks to CDS prices. Unmatched banks are mostly smaller banks from Spain and Eastern Europe that do not have publicly quoted CDS prices. For each bank we match

---

<sup>23</sup>We note that the coefficients are consistent across specifications. For example, in the post-bailout period we find a coefficient of 0.404 in the specification with arithmetic changes. This coefficient is about twice as large as the coefficient (elasticity) in the specification with log CDS changes (Column (9) in Table 3). Given that the elasticity should be the coefficient in the specification with arithmetic changes multiplied by the ratio of bank CDS to sovereign CDS, this implies that the bank CDS should be about twice as large as the sovereign CDS. Indeed, in the post-bailout period the average bank CDS is 188 bps and the average sovereign CDS is 108 bps (Panel B in Table 1).

sovereign holdings to sovereign CDS.

Table 8 presents summary statistics for all banks that participated in the European bank stress tests. As of March 2010, the average bank had risk-weighted assets of 126 billion euros and a Tier 1 capital ratio of 10.2%. The average holdings of gross and net European sovereign bonds are 20.6 billion euros and 19.7 billion euros, respectively. Hence, the average bank holds about one sixth of risk-weighted assets in sovereign bonds. Banks have a strong home bias in their sovereign holdings: about 69.4% of bonds are issued by the country in which a bank is headquartered. This is supportive of the model’s assumption that banks are exposed to home-country sovereign risk through their holdings of government bonds.

We use these data to conduct an alternative test of the impact of sovereign credit risk on bank credit risk. Our test focuses on changes in the value of foreign-sovereign holdings rather than own-country sovereign holdings. The benefit of this approach is that it circumvents the usual concerns about omitted country-specific macro shocks.

To implement this test, we construct a bank-specific variable measuring variation in the value of banks’ *foreign* sovereign bond holdings. Let  $\text{SovBond}_{ik}$  be the share of foreign sovereign holdings of country  $k$  by bank  $i$ . We calculate the foreign holdings variable,  $\text{ForeignBondCDS}_{it}$  as the following weighted average:

$$\text{ForeignBondCDS}_{it} = \sum_{i \neq j} \text{SovBond}_{ik} * \text{SovereignCDS}_{kt}.$$

where  $\text{SovereignCDS}_{kt}$  is the sovereign CDS of country  $k$  on day  $t$ . Note that for each bank the foreign holdings variable excludes home-sovereign bonds. We then estimate the following:

$$\Delta \log(\text{Bank CDS}_{it}) = \delta_t + \gamma \Delta \log(\text{ForeignBondCDS}_{it}) + \varepsilon_{it}. \quad (13)$$

where  $\delta_t$  are time fixed effects. The coefficient of interest is  $\gamma$ , which captures the effect of changes in the value of foreign bond holdings on bank CDS.

We estimate the regressions using the period one month before and one month after the reporting date for the sovereign bond holdings. By estimating this regression, we are implicitly assuming that the marginal CDS investor either knows or at least has some idea of the bank holdings.

Table 9 shows the results. Column (1) shows a positive and statistically significant association between changes in bank CDS and their foreign sovereign holdings. This coefficient suggests that a one-standard deviation increase in the change in the foreign sovereign hold-

ings variable leads to an increase of about half of a one-standard deviation in the change of the bank CDS. Column (2) shows that the coefficient remains unchanged when bank fixed effects are included. Column (3) controls for week fixed effects. The coefficient of interest decreases by about one third but remains statistically significant. This suggests that common shocks affect both the change in bank CDS and the change in the foreign holdings variable. Column (4) controls for day fixed effects. The coefficient decreases by two third relative to the specification without time fixed effects but remains statistically significant at the 1%-level. This result suggests that variation in foreign sovereign holdings contains economically important information about variation in bank credit risk.

To further check for robustness, column (5) adds back bank fixed effects. This does not have any effect on the coefficient. Column (6) estimates the same regression as in Column (5) but excludes the holdings of German bonds from the construction of the foreign-holdings variable. We do this to address a potential concern about reverse causality due to the possibility that Germany may provide bailouts to other countries, or banks in other countries. The column shows that this has no effect on the coefficient of interest.

## 4.5 The Case of Iceland: A Counterfactual?

We end by considering the case of Iceland. As is now well-known, by 2008 the Icelandic banking sector was extremely highly leveraged and very large compared to the size of the Icelandic economy. The three biggest Icelandic banks had active subsidiaries in the UK, Scandinavia, and continental Europe. In late September 2008, fears of a run on the Icelandic banks lead to their being put into receivership under the supervision of the Icelandic government. At the very onset of this crisis, the Icelandic government moved to bailout the first of its failing banks. However, it soon became clear that the government would not be able to save the Icelandic banks under any circumstance. The outstanding debts of the three biggest banks alone included over \$62 billion in foreign currency obligations, which was an order of magnitude bigger than Iceland's 2007 GDP. Facing no possibility of a successful bailout, the Icelandic government separated the domestic and international parts of its banks' operations. It kept the foreign liabilities within the failed lenders and provided *no* support to banks' foreign creditors (either bondholders *or* depositors). Hence, Iceland's banks became effectively bankrupt and indeed still owe creditors \$85 billion today. As the massive scale of these obligations show, it is very clear that Iceland was completely incapable of bailing out its banks. The banking crisis was followed by high inflation, a large

depreciation in the currency, and a severe contraction of the Icelandic economy.

CDS rates on Euro-denominated Icelandic government obligations increased tremendously with the onset of the crisis, reaching well over 1000 bps. This reflected the market's fear that the foreign-currency obligations of the banks would in some ways be taken on by the government, as Iceland's pre-crisis foreign-currency obligations were not very large. The credit-rating agencies precisely expressed this concern as they downgraded Iceland's sovereign debt in 2008, with Moody's stating that "the Icelandic authorities' resolution not to save the whole banking system at the cost of jeopardizing the government's creditworthiness – reflected in decisions damaging to bank creditors' interests – is fraught with operational difficulties", and "some of the banks' external liabilities will eventually filter through to the government's balance sheet" (Moody's Investors Services, 8 October 2008). In this sense, the rise in Icelandic credit risk corresponds well with the model presented by this paper. Since banks obligations were denominated in foreign currency, the Icelandic government would need to fund any transfers in foreign currency as well. The default risk associated with these obligations was reflected in the traded CDS on Euro-denominated Icelandic bonds.

Ultimately, Iceland did *not* take on significant foreign obligations from its banking sector. Perhaps this was due to the tremendous magnitude of these obligations relative to its resources. Within our model, we can interpret this outcome as the corner solution that arises when the government is incapable of increasing the financial sector's probability of solvency ( $p_{solv}$ ) above zero for any level of taxation and corresponding transfer. Under such circumstances it is optimal within the model for the government to avoid increasing outstanding debt or giving any transfer to the financial sector.

Figure 10 shows that subsequently, Iceland CDS rates have decreased tremendously. The figure compares the sovereign CDS of Iceland with that of Ireland. It shows that Iceland CDS rates are now significantly below those of Ireland. Note that, by all estimates, Iceland has experienced a contraction in output that is greater than that of Ireland, so that this difference does not reflect Iceland's greater economic performance over the subsequent period. In that sense, Figure 10 can serve as a counterfactual that provides support for the inference that if sovereigns abstained from financial sector bailouts, they would face lower sovereign credit risk.

## 5 Related literature

Our paper is related to three different strands of literature: (i) the theoretical literature on bank bailouts; (ii) the literature on costs of sovereign default; and, (iii) the recent empirical literature on effects of bank bailouts on sovereigns.

The theoretical literature on bank bailouts has mainly focused on *how* to structure bank bailouts efficiently. While the question of *how* necessarily involves an optimization with some frictions, the usual friction assumed is the inability to resolve failed bank's distress entirely due to agency problems. This could be due to under-investment problem as in our setup (e.g., Philippon and Schnabl, 2009), adverse selection (e.g., Gorton and Huang, 2004), risk-shifting or asset substitution (e.g., Acharya, Shin and Yorulmazer, 2008, Diamond and Rajan, 2009), or tradeoff between illiquidity and insolvency problems (e.g., Diamond and Rajan, 2005). Some other papers (Philippon and Schnabl, 2009, Bhattacharya and Nyborg, 2010, among others) focus on specific claims through which bank bailouts can be structured to limit these frictions.

A large body of existing literature in banking considers that bank bailouts are inherently a problem of time consistency and induce moral hazard at individual-bank level (Mailath and Mester, 1994) and at collective level through herding (Penati and Protopapadakis, 1988, Acharya and Yorulmazer, 2007). Aghion, Bolton and Fries (1999) consider the cost that bank debt restructuring can in some cases delay the recognition of loan losses. Brown and Dinc (2009) show empirically that the governments are more likely to rescue a failing bank when the banking system, as a whole, is weak.

A small part of this literature, however, does consider *ex-post* costs of bailouts. Notably, Diamond and Rajan (2005, 2006) study how bank bailouts can take away a part of the aggregate pool of liquidity from safe banks and endanger them too. Acharya and Yorulmazer (2007, 2008) model, in a reduced-form manner, a cost of bank bailouts to the government or regulatory budget that is increasing in the quantity of bailout funds. They provide taxation-related fiscal costs as a possible motivation. Panageas (2010a,b) considers the optimal taxation to fund bailouts in a continuous-time dynamic setting, also highlighting when banks might be too big to save.

In the theoretical literature on sovereign defaults, Bulow and Rogoff (1989a, 1989b) initiated a body of work that focused on ex-post costs to sovereigns of defaulting on external debt, e.g., due to reputational hit in future borrowing, imposition of international trade sanctions and conditionality in support from multi-national agencies. Broner and Ventura

(2005), Broner, Martin and Ventura (2007), Acharya and Rajan (2010) and Gennaioli, Martin and Rossi (2010), among others, consider a collateral damage to the financial institutions and markets when a sovereign defaults. They employ this as a possible commitment device that gives the sovereign “willingness to pay” its creditors. Our model considers both of these effects, an ex-post deadweight cost of sovereign default in external markets as well as an internal cost to the financial sector through bank holdings of government bonds.

One strand of recent empirical work focuses on the distortionary design of bank bailout packages. Acharya and Sundaram (2009) document how the loan guarantee program of the Federal Deposit Insurance Corporation in the Fall of 2008 was charged in a manner that favored weaker banks at the expense of safer ones, producing a downward revision in CDS spreads of the former. Veronesi and Zingales (2009) conduct an event study and specifically investigate the U.S. government intervention in October 2008 through TARP and calculate the benefits to banks and costs to taxpayers. They find that the government intervention increased the value of banks by over \$100 billion, primarily of bank creditors, but also estimate a tax payer cost between \$25 to \$47 billion. Panetta et al. (2009) and King (2009) assess the Euro zone bailouts and reach the conclusion that while bank equity was wiped out in most cases, bank creditors were backstopped reflecting a waiting game on part of bank regulators and governments.

Another strand of recent empirical work relating financial sector and sovereign credit risk during the ongoing crisis shares some similarity to the very recent papers on this theme. Sgherri and Zoli (2009), Attinasi, Checherita and Nickel (2009) and Ejsing and Lemke (2011) focus on the effect of bank bailout announcements on sovereign credit risk measured using CDS spreads. Some of their evidence mirrors our descriptive evidence. Dieckmann and Plank (2009) analyze sovereign CDS of developed economies around the crisis and document a significant rise in co-movement following the collapse of Lehman Brothers. Demirguc-Kunt and Huizinga (2010) do an international study of equity prices and CDS spreads around bank bailouts and show that some large banks may be too big to save rather than too big to fail. Our analysis corroborates and complements some of this work. In particular, our empirical investigation of banking sector holdings of government debt and how this introduces a linkage between bank CDS and sovereign CDS is novel.

## 6 Conclusion

This paper examines the intimate and intricate link between bank bailouts and sovereign credit risk. We develop a model in which the government faces an important trade-off: bank bailouts ameliorate the under-investment problem in the financial sector but reduce the investment incentives of the non-financial sector due to the corresponding increase in future taxation. In the short-run, bailouts are funded through the issuance of government bonds. A high level of issuance helps to fund the bailout but dilutes existing bondholders and introduces credit risk into the government bond price. This creates a two-way feedback between sovereign and financial sector credit risk because financial firms are exposed to the value of government debt through both their direct bond holdings and via the value of explicit government guarantees or an implicit safety net.

We provide supporting evidence for our model using data from the financial crisis of 2007-10. In particular, we document that developed country governments transferred credit risk from the financial sector to taxpayers during the height of the crisis in October 2008. Using a panel of bank and sovereign CDS we document and quantify the direct two-way feedback between sovereign and bank credit risk. We also collect data on sovereign bond holdings from the European bank stress test in May 2010 and find that the value of foreign sovereign bond holdings is informative about banks' credit risk.

We consider the emergence of meaningful sovereign credit risk as an important potential cost of bank bailouts. This cost is a reflection of the future taxation (or more generally, even inflation risk) imposed on the corporate and household sectors of the economy. This cost of bailouts can render the immediate stabilization of the financial sector a Pyrrhic victory, but it has received little theoretical attention and has also not been analyzed much empirically. Taking cognizance of this ultimate cost of bailouts has important consequences for the future resolution of financial crises, the design of fiscal policy, and the nexus between the two.

## References

- Acharya, Viral V. and Raghuram G. Rajan, 2010, "Financial Sector and Sovereign Credit Risk", Work in progress, New York University Stern School of Business.
- Acharya, Viral, Hyun Song Shin and Tanju Yorulmazer, 2008, "Crisis Resolution and Bank Liquidity", *Review of Financial Studies*, forthcoming.



- Acharya, Viral V. and Rangarajan Sundaram, 2009, “The Financial Sector ‘Bailout’: Sowing the Seeds of the Next Crisis”, Chapter 15 in Acharya, Viral V. and Matthew Richardson (editors), 2009. “Restoring Financial Stability: How to Repair a Failed System”, New York University Stern School of Business, John Wiley & Sons.
- Acharya, Viral V. and Tanju Yorulmazer, 2007 “Too Many to Fail - An Analysis of Time-inconsistency in Bank Closure Policies,” *Journal of Financial Intermediation*, 16(1), 1–31.
- Acharya, Viral V. and Tanju Yorulmazer, 2008, “Cash-in-the-Market Pricing and Optimal Resolution of Bank Failures,” *Review of Financial Studies*, 21, 2705–2742.
- Aghion, Philipp, Patrick Bolton and Steven Fries, 1999, “Optimal Design of Bank Bailouts: The Case of Transition Economies”, *Journal of Institutional and Theoretical Economics*, 155, 51–70.
- Attinasi, Maria-Grazia, Cristina Checherita and Christiane Nickel, 2009, “What Explains the Surge in Euro Area Sovereign Spreads during the Financial Crisis of 2007-09?”, European Central Bank Working Paper No. 1131.
- Bhattacharya, Sudipto and Kjell G. Nyborg, 2010, “Bank Bailout Menus”, Swiss Finance Institute Research Paper Series No. 10–24.
- Broner, Martin and Jaume Ventura, 2005, “Globalization and Risk Sharing”, Working Paper, Universitat Pompeu Fabra.
- Broner, Martin, Alberto Martin and Jaume Ventura, 2007, “Enforcement Problems and Secondary Markets”, Working Paper, Universitat Pompeu Fabra.
- Brown, C. and Dinc, S., 2009, “Too Many to fail? Evidence of regulatory forbearance When the banking sector is weak”, *Review of financial Studies*, forthcoming.
- Bulow, J., and K. Rogoff, 1989a, “Sovereign debt: Is to forgive to forget?”, *American Economic Review*, 79, 43-50.
- Bulow, J., and K. Rogoff, 1989b, “A constant recontracting model of sovereign debt”, *Journal of Political Economy*, 97, 155-178.
- Collin-Dufresne, Pierre, Robert S. Goldstein and J. Spencer Martin, 2001, “The Determinants of Credit Spread Changes”, *Journal of Finance*, 56(6), 2177-2207.

- Demirguc-Kunt, Asli and Harry Huizinga, 2010, “Are Banks Too Big to Fail or Too Big to Save? International Evidence from Equity Prices and CDS Spreads”, World Bank Policy Research Working Paper 5360.
- Diamond, Douglas and Raghuram G. Rajan, 2005, “Liquidity Shortages and Banking Crises”, *Journal of Finance*, 60(2), 615–647.
- Diamond, Douglas and Raghuram G. Rajan, 2006, “Bank Bailouts and Aggregate Liquidity”, *American Economic Review Papers and Proceedings*, 92(2), 38–41.
- Diamond, Douglas and Raghuram G. Rajan, 2009, “Fear of Fire Sales, Illiquidity Seeking and Credit Freeze”, *Quarterly Journal of Economics*, forthcoming.
- Dieckmann, Stephan and Thomas Plank, 2009, “Default Risk of Advanced Economies: An Empirical Analysis of Credit Default Swaps during the Financial Crisis”, Working Paper, Wharton School of Business, University of Pennsylvania.
- Ejsing, Jacob and Wolfgang Lemke, 2011, The Janus-headed salvation: Sovereign and bank credit risk premia during 2008–2009, *Economics Letters*, 110, 28–31.
- Gennaioli, Nicola, Alberto Martin and Stefano Rossi, 2010, “Sovereign Default, Domestic Banks and Financial Institutions,” Working Paper, Universitat Pompeu Fabra.
- Gorton, Gary and Lixin Huang. 2004. Liquidity, Efficiency, and Bank Bailouts. *American Economic Review*, 94(3): 455–483.
- King, Michael R, 2009, “Time to Buy or Just Buying Time? The Market Reaction to Bank Rescue Packages”, BIS Papers No 288 (September).
- Mailath, George and Loretta Mester, 1994, “A Positive Analysis of Bank Closure,” *Journal of Financial Intermediation*, 3(3), 272–299.
- Merton, Robert C., 1974, “On the Pricing of Corporate Debt: The Risk Structure of Interest Rates,” *Journal of Finance*, 29, 449–470.
- Moody’s Investors Services, 8 October 2008, ”Moody’s downgrades Iceland’s ratings to A1 from Aa1,”.
- Myers, Stewart C., 1977, “The Determinants of Corporate Borrowing,” *Journal of Financial Economics*, 5(2), 147–175.

- Panageas, Stavros, 2010a, “Optimal taxation in the presence of bailouts”, *Journal of Monetary Economics*, 57, 101?-116.
- Panageas, Stavros, 2010b, “Bailouts, the incentive to manage risk, and financial crises”, *Journal of Financial Economics*, 95, 296?-311.
- Panetta, Faib, Thomas Faeh, Giuseppe Grande, Corrinne Ho, Michael King, Aviram Levy, Federico M Signoretti, Marco Taboga, and Andrea Zaghini, 2009, “An Assessment of Financial Sector Rescue Programmes”, BIS Papers No 48 (July).
- Penati, A. and Protopapadakis, A., 1988, “The effect of implicit deposit insurance on banks? portfolio choices, with an application to international overexposure”, *Journal of Monetary Economics*, 21(1), 107–126.
- Veronesi, P. and Zingales, L., 2009, “Paulson’s Gift”, *Journal of Financial Economics*, forthcoming.
- Philippon, Thomas and Philipp Schnabl, 2009, “Efficient Recapitalization”, Working Paper, New York University Stern School of Business.
- Sgherri, Silvia and Edda Zoli, 2009, “Euro Area Sovereign Risk During the Crisis”, Working paper, International Monetary Fund, No. 09–222.

Figure 1: Sovereign CDS and Bank CDS of Ireland

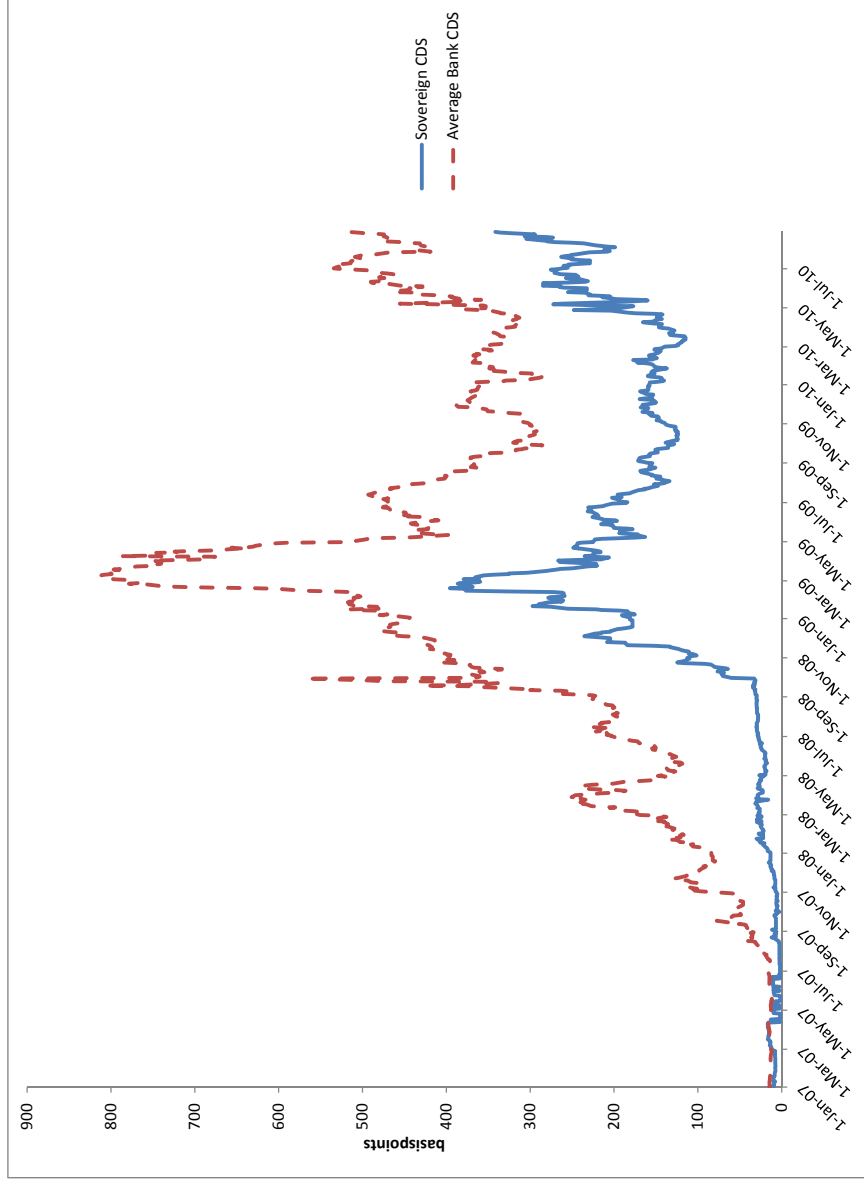


Figure 1 plots the sovereign CDS and bank CDS for Ireland in the period from 3/1/2007 to 8/31/2010. The bank CDS is computed as the unweighted average of bank CDS for banks headquartered in Ireland (Allied Irish Bank, Anglo Irish Bank, Bank of Ireland, and Irish Life and Permanent). The data are from Datastream.

Figure 2: The Default Boundary (Certainty Case)

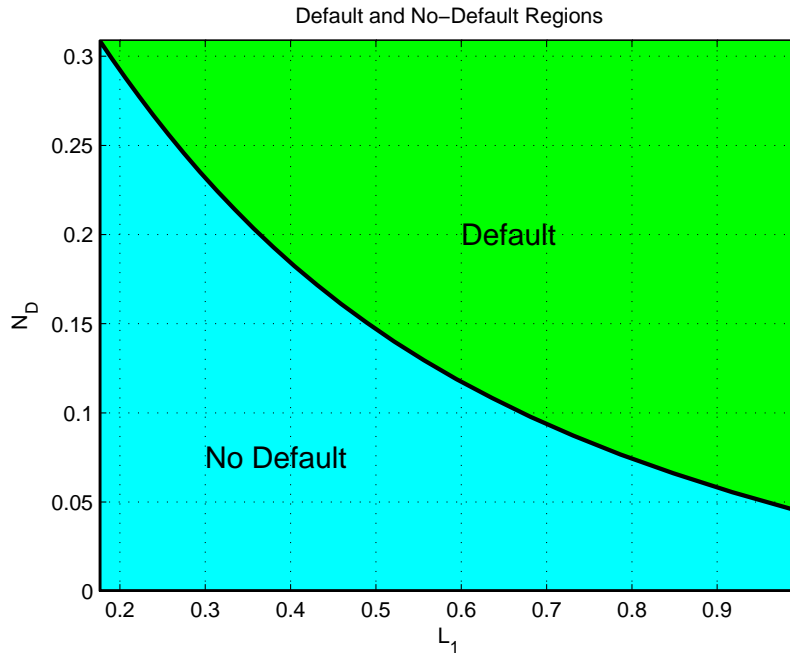
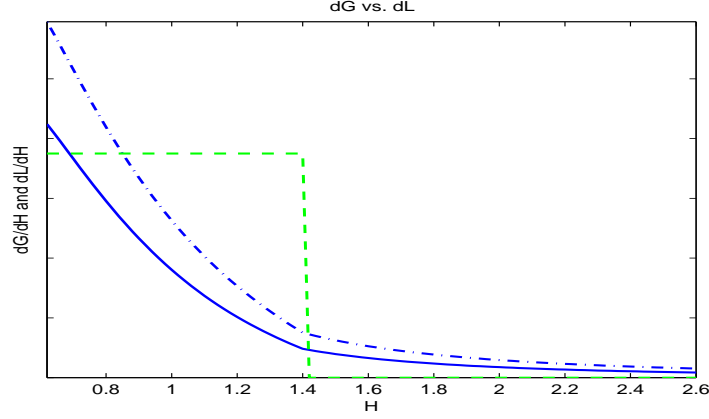
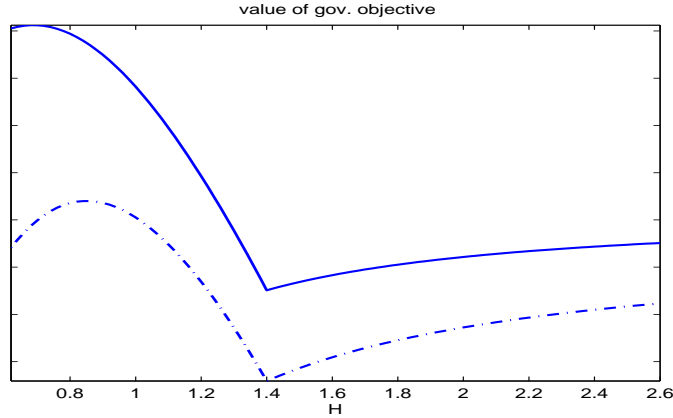


Figure 2 shows the Default and No-Default Regions in the space of  $L_1 \times N_D$  (financial sector leverage/debt overhang  $\times$  pre-existing sovereign debt) for the model under certainty. The black curve separating these two regions gives the default boundary. The plot corresponds to a parameterization of the model where  $\tilde{A}_1 \sim U[0, 1]$ ,  $L_1 = 0.5$ ,  $\alpha = 1$ ,  $\vartheta = 0.3$ ,  $\gamma = 0.2$ ,  $\beta = 0.5$ ,  $m = 1.3$ ,  $D = 0.02$ ,  $k = 0$ , and  $N_D = 0.25$  (solid line).

Figure 3: Marginal Gain and Loss of Increasing  $H$

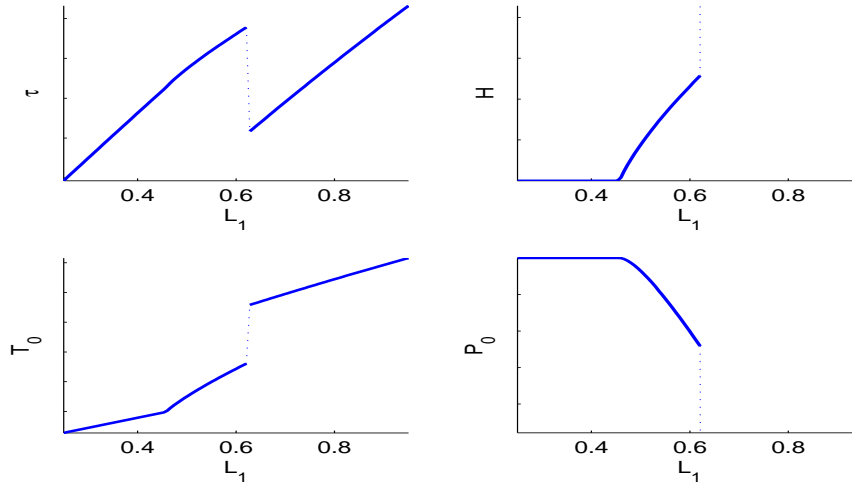


Value of Government's Objective Function



The top panel of Figure 3 plots the marginal gain of increasing  $H$  while holding constant  $\mathcal{T}$ ,  $d\mathcal{G}/dH$  (solid line and dash-dot line) and the resulting marginal increase in expected dead-weight default cost  $D \frac{dpdef}{dH}$  (dashed line). Uncertainty over growth/tax revenues,  $\tilde{R}_V$ , is assumed to have a uniform distribution. The dash-dot line corresponds to a higher level of  $L_1$  than for the solid line. The bottom panel of the Figure shows the resulting value of the government's objective function, with the the solid and dash-dot line corresponding to their counterparts in the top panel. The plots correspond to a parameterization of the model where  $\tilde{R}_V \sim U[0.6, 1.4]$ ,  $\tilde{A}_1 \sim U[0, 1]$ ,  $L_1 = 0.5$  (solid line),  $\alpha = 1$ ,  $\vartheta = 0.3$ ,  $\gamma = 0.2$ ,  $\beta = 0.5$ ,  $m = 1.3$ ,  $D = 0.06$ ,  $k = 0$ , and  $N_D = 0.25$ .

Figure 4: Comparative Statics for  $L_1$



Comparative Statics for  $N_D$

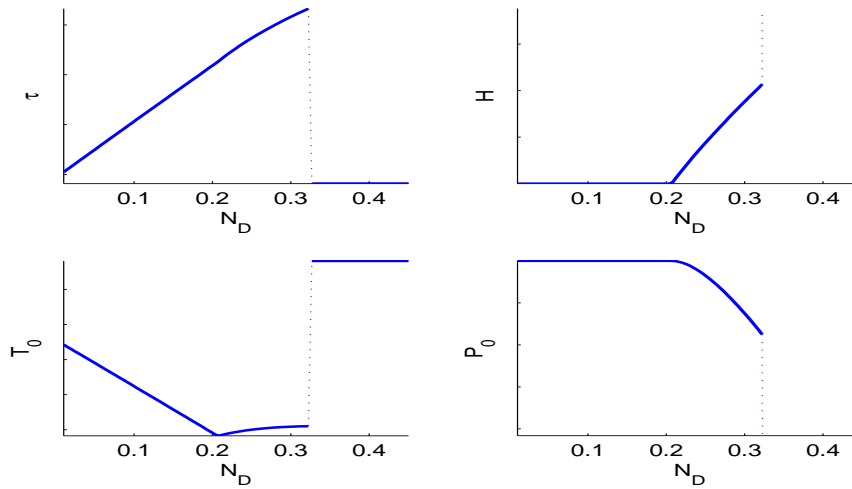


Figure 4 plots the equilibrium values of  $\mathcal{T}$  (expected tax revenue),  $H$ ,  $T_0$  (the transfer), and  $P_0$  (price of sovereign bond) as  $L_1$  (top panel) and  $N_D$  (bottom panel) are varied. The dotted line in the plots represents the point at which total default ( $H \rightarrow \infty$ ) is optimal, resulting in a discontinuity in the plot. The parameters of the model correspond to those in Figure 3.

Figure 5: Change in Sovereign and Bank CDS before Bank Bailouts

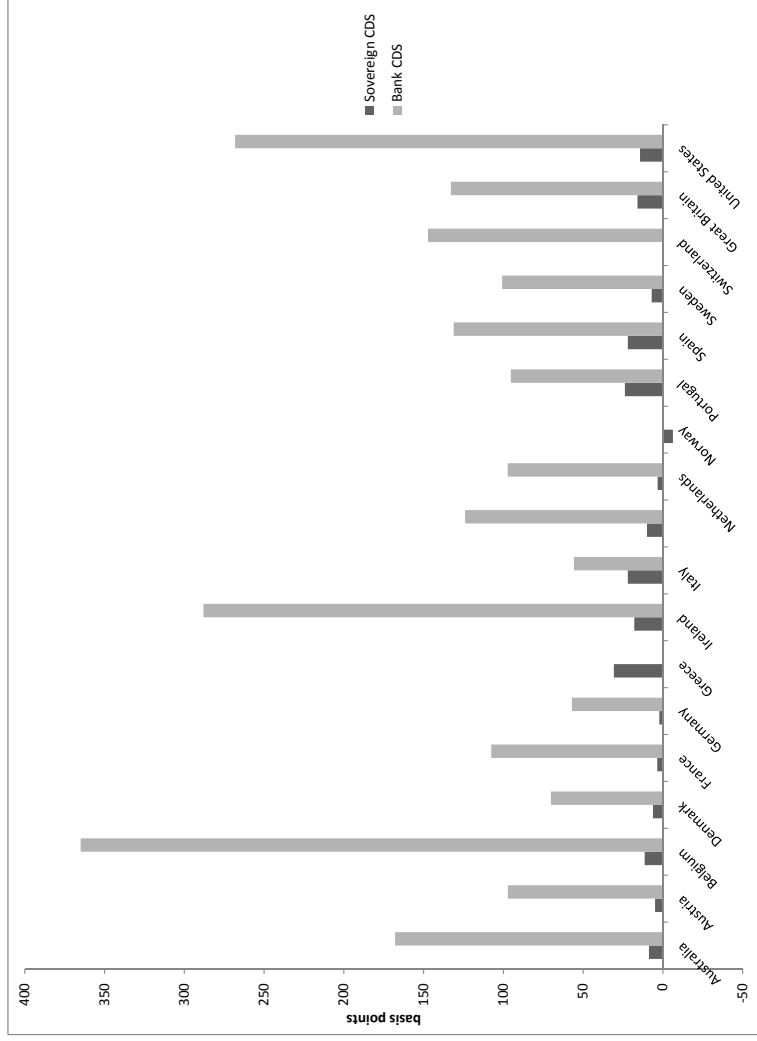


Figure 5 plots the change in average bank CDS and sovereign CDS for Western European countries in the period from 1/1/2007 to 9/25/2008. The bank CDS is computed as the unweighted average of bank CDS for banks headquartered in that country. The data are from Datastream (no data available for Swiss sovereign CDS and Greek bank CDS).



Figure 6: Change in Sovereign and Bank CDS during the Period of Bank Bailouts

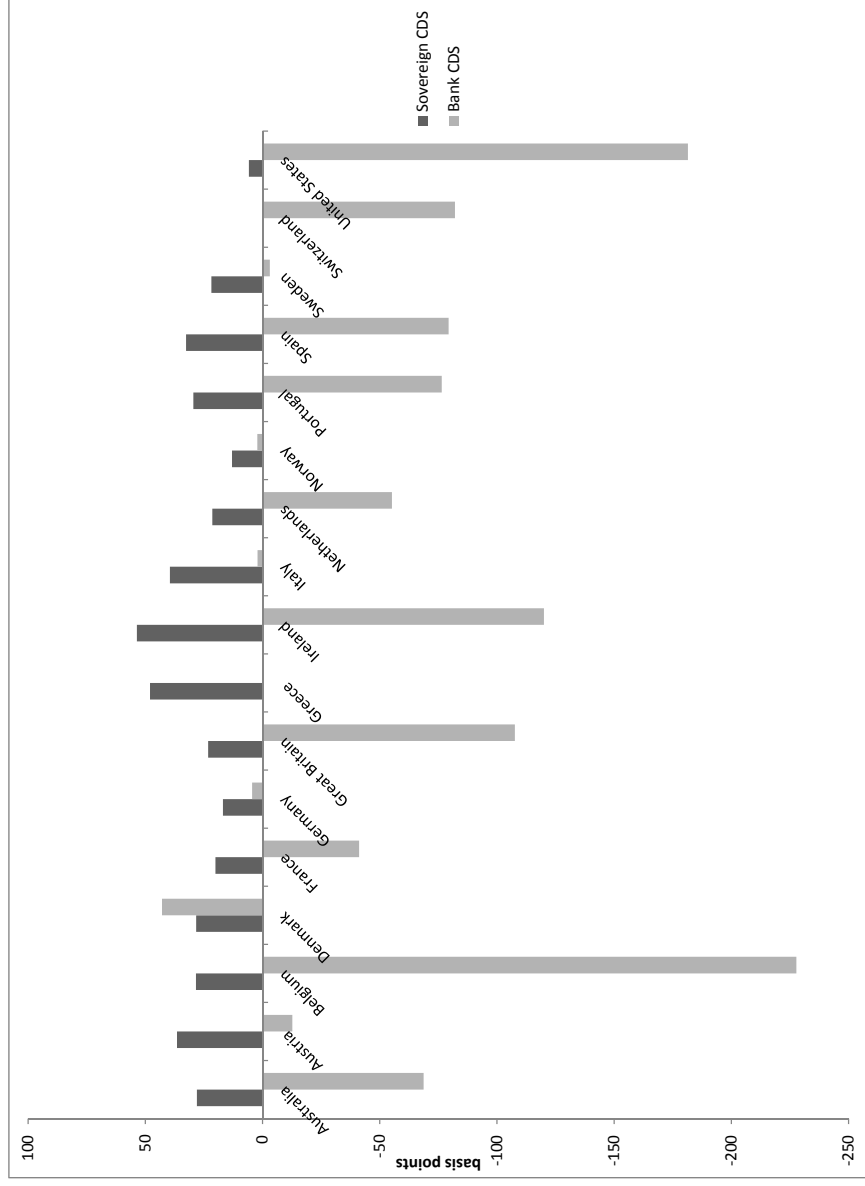


Figure 6 plots the change in average bank CDS and sovereign CDS for Western European countries in the period from 9/26/2008 to 10/21/2008. The bank CDS is computed as the unweighted average of bank CDS for banks headquartered in that country. The data are from Datastream (no data available for Swiss sovereign CDS and Greek bank CDS).

Figure 7: Change in Sovereign and Bank CDS after Bank Bailouts

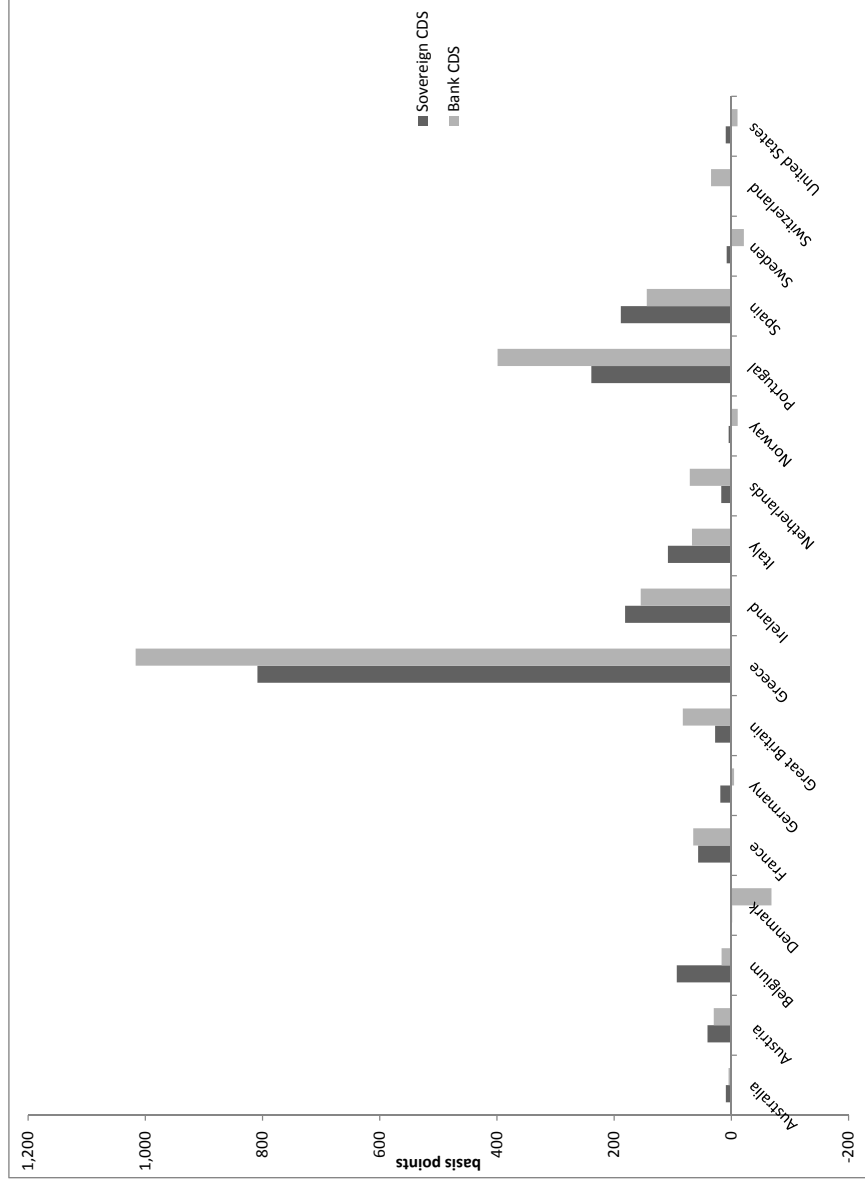


Figure 7 plots the change in average bank CDS and sovereign CDS for Western European countries in the period from 10/22/2008 to 6/30/2010. The bank CDS is computed as the unweighted average of bank CDS for banks headquartered in that country. The data are from Datastream.

Figure 8: Correlation between Sovereign CDS and Public Debt before and after Bank Bailouts

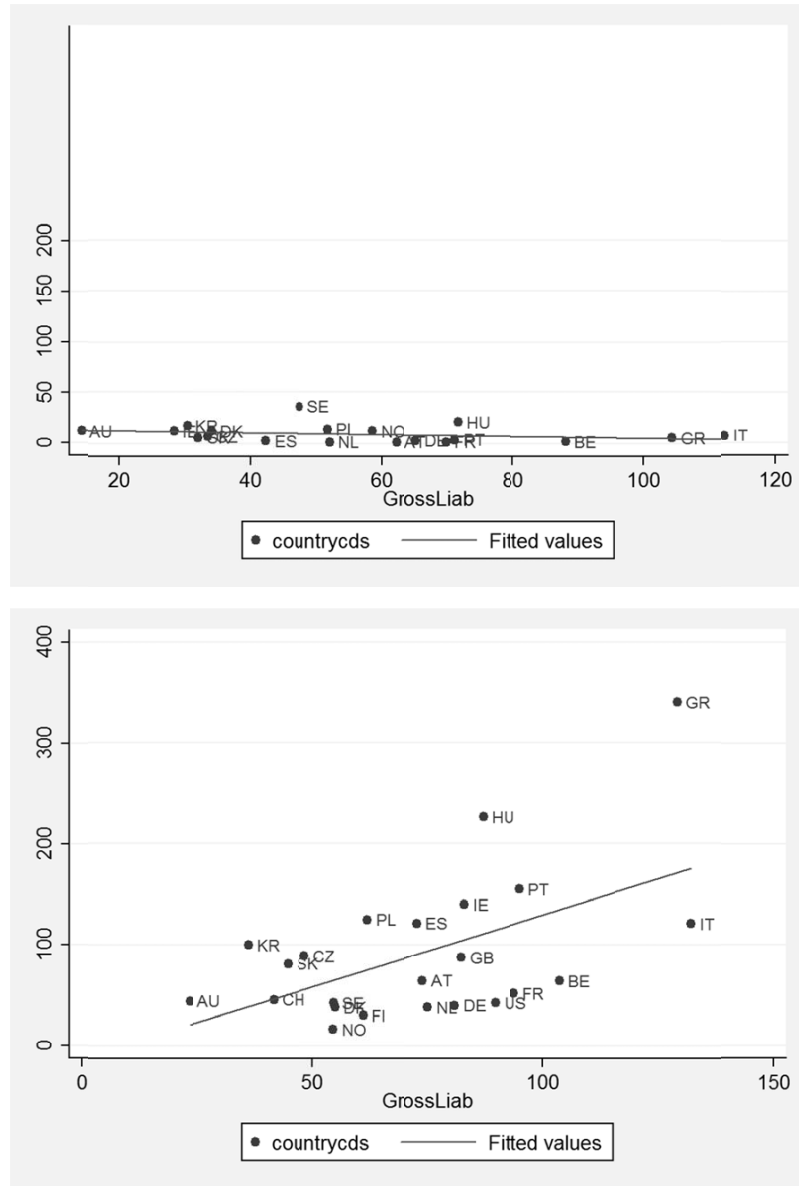


Figure 8 shows the correlation between sovereign CDS and public liabilities (as a percentage of GDP) for Western European countries before and after the bank bailouts. The top figure shows no correlation before the bailouts (as of 3/1/2007). The bottom figure shows a strong correlation after the bank bailouts (as of 3/1/2010). The CDS data are from Datastream and the public liabilities data are from the OECD Economic Outlook database.

Figure 9: Correlation of Bank and Sovereign CDS

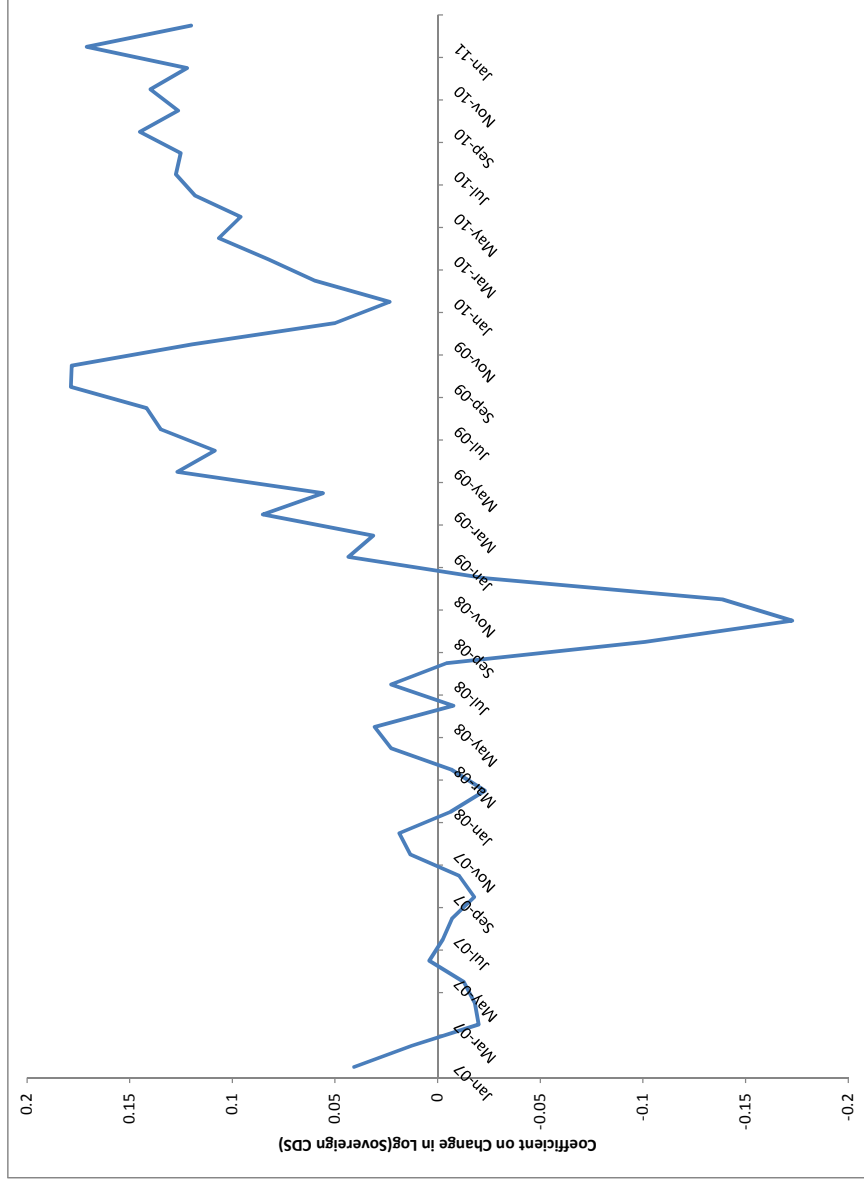


Figure 9 plots the three-month moving average of the coefficients on the interaction of year-month fixed-effects and the change in sovereign CDS from the main regression model (includes all controls).

Figure 10: Sovereign CDS of Iceland and Ireland

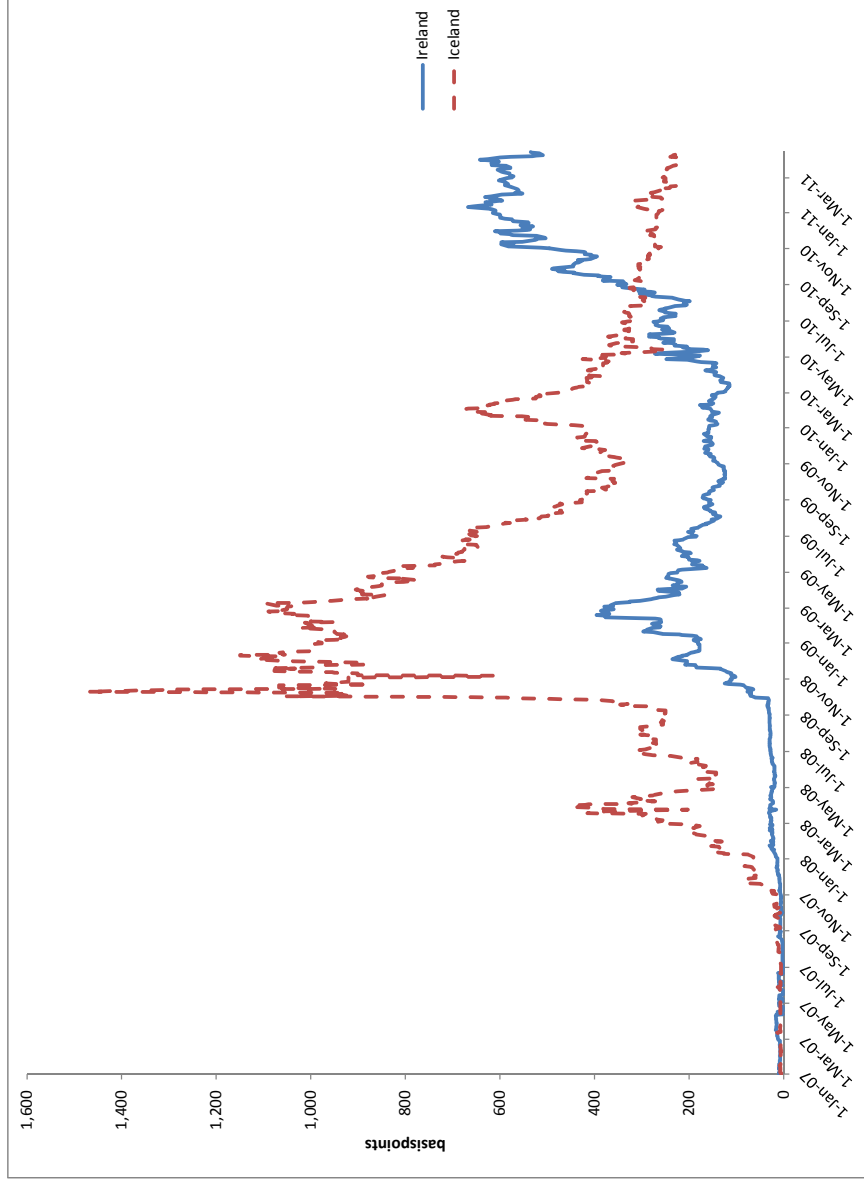


Figure 10 plots the sovereign CDS of Iceland and Ireland in the period from 3/1/2007 to 4/30/2011. The data are from Datastream.

**Table 1: Summary Statistics**

The sample shows summary statistics on bank and sovereign credit risk. The sample includes all European, U.S., and Australian banks with available data on bank CDS, sovereign CDS, and equity returns. The data are at the weekly level. Panel A presents summary statistics for the first week of July 2007. Panel B presents summary statistics for the period before, around, and after the bailouts.

Panel A: Cross-Section (7/1/2007)						
	#	Mean	Std.Dev	50 <sup>th</sup> percentile	5 <sup>th</sup> percentile	95 <sup>th</sup> percentile
Assets (\$ billion)	81	589.3	594.9	362.6	77.9	1,896.90
Equity (\$ billion)	81	26.8	29.3	20.2	3.5	112.4
Equity Ratio (%)	81	5.1	2.7	4.8	1.9	10
Tier 1 Ratio (%)	66	8.5	1.9	8.2	6.5	12.4
Bank CDS (bp)	75	21.8	13.4	10.5	6.5	41
Sovereign CDS (bp)	56	6.6	11.5	2	1.5	52.1
Panel B: Time-Series						
Pre-Bailout (1/1/2007-9/17/2008)						
	#	Mean	Std.Dev	50 <sup>th</sup> percentile	5 <sup>th</sup> percentile	95 <sup>th</sup> percentile
Bank CDS (bp)	2,891	93.2	129	67.7	6.6	271.2
Sovereign CDS (bp)	2,891	13.5	12.1	9.6	1.8	38.3
$\Delta$ Bank CDS (%)	2,891	0.038	0.247	0.025	-0.242	0.329
$\Delta$ Sovereign CDS (%)	2,891	0.024	0.3	0.028	-0.256	0.318
Bank Stock Return (%)	2,891	-0.011	0.084	-0.006	-0.116	0.081
$\Delta$ CDS Market Index (%)	2,891	0.021	0.118	0.005	-0.141	0.211
$\Delta$ Volatility (%)	2,891	0.003	0.032	0.002	-0.038	0.043
Bailout (9/18/2008-10/22/2008)						
Bank CDS (bp)	254	288.6	626.0	133.3	70.0	740.0
Sovereign CDS (bp)	254	39.3	18.8	32.5	12.5	73.5
$\Delta$ Bank CDS (%)	254	-0.065	0.44	-0.037	-0.629	0.405
$\Delta$ Sovereign CDS (%)	254	0.146	0.19	0.129	-0.105	0.502
Bank Stock Return (%)	254	-0.067	0.268	-0.03	-0.374	0.201
$\Delta$ CDS Market Index (%)	254	0.017	0.095	0.04	-0.157	0.116
$\Delta$ Volatility (%)	254	0.048	0.071	0.076	-0.036	0.127
Post-Bailout (10/23/2008 - 30/4/2011)						
Bank CDS (bp)	6,500	188.7	179.9	131.2	65.5	560.6
Sovereign CDS (bp)	6,500	108.5	142.9	60.1	24.9	347
$\Delta$ Bank CDS (%)	6,500	0.003	0.12	-0.001	-0.158	0.184
$\Delta$ Sovereign CDS (%)	6,500	0.004	0.113	0.003	-0.181	0.186
Bank Stock Return (%)	6,500	0	0.098	0.002	-0.132	0.129
$\Delta$ CDS Market Index (%)	6,500	-0.002	0.071	-0.006	-0.113	0.117
$\Delta$ Volatility (%)	6,500	-0.003	0.048	-0.004	-0.059	0.06

**Table 2: Emergence of Sovereign Credit Risk**

This table shows the relation between sovereign credit risk, public debt-to-gdp, and financial sector distress. The sample includes Australia, Denmark, Great Britain, Norway, Sweden, Switzerland, and all Eurozone countries with publicly available data on sovereign CDS and bank CDS. The data are at the country-level. The independent variable in Columns (1) and (2) is the sovereign CDS before the bank bailouts (as of 1/1/2008). Columns (1) and (2) control for Pre-bailout Debt (debt-to-gdp ratio) measured as Government Liabilities as share of GDP (collected from the OECD Economic Outlook). Column (2) controls for financial sector distress measured as the natural logarithm of the average banks CDS before the bank bailouts (as of 9/22/2008). The independent variable in Columns (3) and (4) is the sovereign CDS after the bank bailouts (as of 3/31/2010). The dependent variables are the same as in Columns (1) and (2), respectively. The independent variable in Column (5) is the change in the debt-to-gdp ratio from June 2008 to June 2010. The dependent variable is financial sector distress. The independent variable in column (6) is the debt-to-gdp ratio in June 2010. The dependent variables are the pre-bailout debt-to-GDP ratio and financial sector distress. We report robust standard errors. \*\* 1% significant, \* 5% significant, and + 10% significant

	Log (Sovereign CDS)				Debt-to-GDP	
	Pre-Bailout		Post-Bailout		Post-Bailout	
	1/1/2008		3/31/2010		$\Delta$ 2008-2010	3/31/2010
	(1)	(2)	(3)	(4)	(5)	(6)
Pre-Bailout Debt-to-GDP	0.006 (0.004)	0.005 (0.005)	0.015* (0.006)	0.013+ (0.007)		1.107** (0.144)
Pre-Bailout Financial Sector Distress		0.311 (0.208)		0.965* (0.357)	20.118+ (10.168)	21.726+ (11.555)
Constant	2.137** (0.320)	0.601 (1.154)	3.112** (0.401)	-1.593 (2.019)	-86.920 (49.456)	-101.548 (60.923)
Observations	15	14	17	15	15	15
R-squared	0.134	0.171	0.261	0.488	0.364	0.843

**Table 3: Change in Bank and Sovereign Credit Risk**

This table shows the effect of sovereign credit risk on bank credit risk during the financial crisis. The sample includes all European, U.S., and Australian banks with available data on bank and sovereign CDS. The data are at the weekly level. Columns (1) to (3) cover the pre-bailout period (1/1/2007-9/17/2008), Columns (4) to (6) cover the bailout period (9/18/2008-10/22/2008), and Columns (7) to (9) cover the post-bailout period (10/23/2008-04/30/2011). The dependent variable is the weekly change in the natural logarithm of bank CDS. The main independent variable is the weekly change in the sovereign CDS. The sovereign CDS is assigned based on the country where the bank is headquartered. The control variables are the change in the CDS market index and the volatility index. Columns (2), (3), (5), (6), (8), and (9) include week fixed effects. Column (3), (6), (9) include bank fixed effects and interactions of bank fixed effects with the change in CDS market index and the volatility index. The standard errors are clustered at the bank-level. \*\* 1% significant, \* 5% significant, and + 10% significant

	$\Delta \text{ Log(Bank CDS)}$								
	Pre-Bailout			Bailout			Post-Bailout		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
$\Delta \text{ Log(Sovereign CDS)}$	0.017 (0.010)	0.003 (0.016)	0.003 (0.017)	0.448* (0.169)	-0.715* (0.282)	-1.293** (0.387)	0.221** (0.026)	0.163** (0.035)	0.163** (0.033)
$\Delta \text{ Log(CDS Market Index)}$	0.962** (0.043)			0.893** (0.216)			0.722** (0.034)		
$\Delta \text{ Volatility Index}$	0.671** (0.113)			-0.946** (0.238)			0.057 (0.051)		
Week FE	N	Y	Y	N	Y	Y	N	Y	Y
Interactions	N	N	Y	N	N	Y	N	N	Y
Observations	2,891	2,891	2,891	254	254	254	6,500	6,500	6,500
Banks	62	62	62	53	53	53	59	59	59
R-squared	0.262	0.344	0.476	0.114	0.256	0.599	0.338	0.414	0.479



**Table 4: Change in Bank and Sovereign Credit Risk (controlling for Equity Return)**

This table shows the effect of sovereign credit risk on bank credit risk during the financial crisis. The sample includes all European, U.S., and Australian banks with available data on bank CDS, sovereign CDS, and equity returns. The data are at the weekly level. Columns (1) to (3) cover the pre-bailout period (1/1/2007-9/17/2008), Columns (4) to (6) cover the bailout period (9/18/2008-10/22/2008), and Columns (7) to (9) cover the post-bailout period (10/23/2008-04/30/2011). The dependent variable is the weekly change in the natural logarithm of bank CDS. The main independent variable is the weekly change in the sovereign CDS. The sovereign CDS is assigned based on the country where the bank is headquartered. The control variables are the change in the CDS market index, the change in the volatility index, and equity return. Columns (2), (3), (5), (6), (8), and (9) include week fixed effects. Column (3), (6), (9) include bank fixed effects and interactions of bank fixed effects with the change in CDS Market index, the change in volatility index, and equity return. The standard errors are clustered at the bank-level. \*\* 1% significant, \* 5% significant, and + 10% significant

	$\Delta \text{ Log(Bank CDS)}$								
	Pre-Bailout			Bailout			Post-Bailout		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
$\Delta \text{ Log(Sovereign CDS)}$	0.014 (0.010)	0.003 (0.016)	0.004 (0.018)	0.449** (0.164)	-0.691** (0.257)	-1.020 (1.034)	0.197** (0.028)	0.153** (0.036)	0.146** (0.033)
Equity Return	-0.306* (0.142)	-0.211 (0.140)		-0.194 (0.185)		-0.911 (2.602)	-0.145** (0.030)	-0.095** (0.030)	
$\Delta \text{ Log(CDS Market Index)}$	0.932** (0.048)			0.753** (0.200)			0.688** (0.031)		
$\Delta \text{ Volatility Index}$	0.429** (0.134)			-1.100** (0.207)			-0.027 (0.052)		
Week FE	N	Y	Y	N	Y	Y	N	Y	Y
Interactions	N	N	Y	N	N	Y	N	N	Y
Observations	2,891	2,891	2,891	254	254	254	6,500	6,500	6,500
Banks	62	62	62	53	53	53	59	59	59
R-squared	0.271	0.347	0.517	0.126	0.259	0.854	0.349	0.417	0.495

**Table 5: Change in Bank and Sovereign Credit Risk (by Tier 1 Capital)**

This table shows the effect of sovereign credit risk on bank credit risk during the financial crisis. The sample includes all European, U.S., and Australian banks with available data on bank CDS and share prices. The data are at the weekly level. Columns (1) to (3) cover the pre-bailout period (1/1/2007-9/17/2008), Columns (4) to (6) cover the bailout period (9/18/2008-10/22/2008), and Columns (7) to (9) cover the post-bailout period (10/23/2008-04/30/2011). The dependent variable is the weekly change in the natural logarithm of bank CDS. The Tier 1 capital ratio is the regulatory bank capital ratio. All other variables are defined in Tables 3 to 5. The regression includes the Tier 1 capital ratio and an interaction between the Tier1 capital ratio and the change in sovereign CDS. All other controls are the same as in Table 4. The standard errors are clustered at the bank-level. \*\* 1% significant, \* 5% significant, and + 10% significant

	$\Delta \text{ Log(Bank CDS)}$								
	Pre-Bailout			Bailout			Post-Bailout		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
$\Delta \text{ Log(Sovereign CDS)*Tier 1}$	0.005 (0.006)	-0.000 (0.005)	0.003 (0.007)	-0.114 (0.096)	-0.090 (0.089)	-0.035 (0.298)	-0.026 (0.018)	-0.025 (0.017)	-0.033+ (0.017)
$\Delta \text{ Log(Sovereign CDS)}$	-0.030 (0.048)	0.006 (0.050)	-0.016 (0.069)	1.284 (0.772)	-0.040 (0.840)	-1.029 (2.447)	0.432** (0.150)	0.375* (0.143)	0.436** (0.139)
Tier 1	-0.002 (0.003)	-0.001 (0.003)		0.027+ (0.014)	0.021 (0.014)		-0.000 (0.001)	-0.000 (0.001)	
Equity Return	-0.418** (0.103)	-0.360* (0.154)		-0.574 (0.520)	-0.454 (0.553)		-0.137** (0.034)	-0.086* (0.034)	
Other Controls	Y	Y	Y	Y	Y	Y	Y	Y	Y
Week FE	N	Y	Y	N	Y	Y	N	Y	Y
Interactions	N	N	Y	N	N	Y	N	N	Y
Observations	2,262	2,262	2,262	198	198	198	5,154	5,154	5,154
Bank	48	48	48	41	41	41	47	47	47
R-squared	0.248	0.322	0.492	0.157	0.294	0.852	0.351	0.419	0.489

**Table 6: Equity Return and Change in Sovereign Credit Risk**

This table shows the effect of sovereign credit risk on bank stock returns during the financial crisis. The sample includes all European, U.S., and Australian banks with available data on sovereign CDS and equity returns. The data are at the weekly level. Columns (1) to (3) cover the pre-bailout period (1/1/2007-9/17/2008), Columns (4) to (6) cover the bailout period (9/18/2008-10/22/2008), and Columns (7) to (9) cover the post-bailout period (10/23/2008-04/30/2011). The dependent variable is the equity return. The main independent variable is the weekly change in the sovereign CDS. The sovereign CDS is assigned based on the country where the bank is headquartered. The control variables are the change in the CDS market index and the volatility index. Columns (2), (3), (5), (6), (8), and (9) include week fixed effects. Column (3), (6), (9) include bank fixed effects and interactions of bank fixed effects with the change in CDS market index and the volatility index. The standard errors are clustered at the bank-level. \*\* 1% significant, \* 5% significant, and + 10% significant

	Equity Return								
	Pre-Bailout			Bailout			Post-Bailout		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
$\Delta$ Log(Sovereign CDS)	-0.008*	0.001	0.001	0.001	0.234+	0.225	-0.163**	-0.098**	-0.096**
	(0.004)	(0.003)	(0.003)	(0.072)	(0.140)	(0.190)	(0.019)	(0.018)	(0.017)
$\Delta$ Log(CDS Market Index)	-0.100**			-0.720**			-0.235**		
	(0.017)			(0.072)			(0.015)		
$\Delta$ Volatility Index	-0.792**			-0.793**			-0.575**		
	(0.063)			(0.131)			(0.037)		
Week FE	N	Y	Y	N	Y	Y	N	Y	Y
Bank FE	N	N	Y	N	N	Y	N	N	Y
Interactions	N	N	Y	N	N	Y	N	N	Y
Observations	2,891	2,891	2,891	254	254	254	6,500	6,500	6,500
Banks	62	62	62	53	53	53	59	59	59
R-squared	0.155	0.344	0.417	0.142	0.172	0.706	0.259	0.455	0.494

**Table 7: Change in Bank and Sovereign Credit Risk – Robustness (daily data)**

This table replicates Table 3 (Panel A) and Table 4 (Panel B) for daily data instead of weekly data. We replace week fixed effects with day fixed effects. The coefficients on the control variables are not shown. \*\* 1% significant, \* 5% significant, and + 10% significant

Panel A: Main Specification									
	Pre-Bailout			Bailout			Post-Bailout		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
$\Delta$ Log(Sovereign CDS)	0.004 (0.006)	-0.005 (0.010)	-0.005 (0.010)	-0.166 (0.100)	-0.380** (0.114)	-0.367* (0.167)	0.209** (0.019)	0.105** (0.023)	0.099** (0.022)
Day FE	N	Y	Y	N	Y	Y	N	Y	Y
Interactions	N	N	Y	N	N	Y	N	N	Y
Observations	10,673	10,673	10,673	1,017	1,017	1,017	28,736	28,736	28,736
Banks	62	62	62	53	53	53	59	59	59
R-squared	0.115	0.216	0.240	0.092	0.227	0.350	0.249	0.345	0.383
Panel B: Controlling for Equity									
	Pre-Bailout			Bailout			Post-Bailout		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
$\Delta$ Log(Sovereign CDS)	0.003 (0.006)	-0.006 (0.010)	-0.005 (0.010)	-0.137 (0.105)	-0.389** (0.105)	-0.371** (0.119)	0.193** (0.019)	0.098** (0.022)	0.093** (0.020)
Day FE	N	Y	Y	N	Y	Y	N	Y	Y
Interactions	N	N	Y	N	N	Y	N	N	Y
Observations	10,673	10,673	10,673	1,017	1,017	1,017	28,736	28,736	28,736
Banks	62	62	62	53	53	53	59	59	59
R-squared	0.124	0.220	0.255	0.150	0.249	0.703	0.258	0.349	0.401

**Table 8: Summary Statistics of European Bank Stress Test Sample**

The table shows summary statistics for all banks that participated in the EU Bank Stress Tests from July 2010. The data was collected from the website of the Committee of European Banking Regulators and nation websites of the respective bank regulators. The sovereign holdings are computed as the total value of sovereign holdings relative to risk-weighted assets. We report both the gross and net exposure as reported to bank regulators. The share of trading book and banking book are the share of sovereign holdings held in the respective book. The shares are computed based on gross exposure (net exposure was not reported).

Sovereign Holdings						
Euro Bank Stress Tests Sample, March 31, 2010						
	N	Mean	Std.Dev	50th Percentile	5th Percentile	95th Percentile
	(1)	(2)	(3)	(4)	(5)	(6)
<b>Bank Characteristics</b>						
Risk-weighted Assets (EUR million)	91	126,337	179,130	63,448	3,269	493,307
Tier 1 Capital Ratio (%)	91	10.2	2.4	9.8	7.2	14.4
<b>Sovereign Exposure</b>						
Sovereign Holdings (gross, EUR million)	91	20,668	27,948	7,930	105	81,765
Sovereign Holdings (net, EUR million)	91	19,719	27,329	6,960	105	78,959
Home Sovereign Holdings (gross, EUR million)	91	11,493	14,422	5,774	182	42,800
Home Sovereign Holdings (net, EUR million)	91	11,023	13,956	5,348	117	42,800
Home Share (%)	91	69.4	30.0	81.6	18.9	100
Greek Sovereign Holdings	91	669	2,844	0	0	5,601
Share Banking Book (%)	91	84.9	19.9	92.2	35.4	100.0

**Table 9: Summary Statistics of European Bank Stress Test Sample**

The table shows regression of change in bank CDS on change in exposure to sovereign bank holdings. The sovereign bond holdings data were collected from the website of the Committee of European Banking Regulators and nation websites of the respective bank regulators. We construct the exposure variable as the weighted average of country CDS with sovereign holdings as weights. Changes are computed as log changes. The data covers the period from 3/1/2010 to 4/30/2010. Columns (2), (5) and (6) include bank fixed effects. Column (3) includes week fixed effects. Column (4) to (6) include day fixed effect. The exposure variable in Column (6) excludes German bonds. The standard errors are clustered at the bank-level (51 banks). \*\* 1% significant, \* 5% significant, and +10% significant

Sample	Change in Bank CDS					Excluding Germany (6)
	All (1)	All (2)	All (3)	All (4)	All (5)	
Change in Sovereign Exposure	0.325** (0.027)	0.326** (0.028)	0.261** (0.027)	0.141** (0.049)	0.135** (0.046)	0.137** (0.046)
Bank FE	N	Y	N	N	Y	Y
Week FE	N	N	Y	N	N	N
Day FE	N	N	N	Y	Y	Y
Observations	2,317	2,317	2,317	2,317	2,317	2,317
Banks	51	51	51	51	51	0.357
R-squared	0.173	0.188	0.228	0.342	0.357	0.357
Adjusted R-Squared	0.173	0.170	0.224	0.329	0.329	0.329